

A.1.

Marks obtained	Frequency	Cumulative frequency
0-10	8	8
10-20	10	18
20-30	12	30
30-40	22	52
40-50	30	82
50-60	18	100

Here Total no. of observations = 100 = n.

$$\frac{n}{2} = 50.$$

∴ Median class is 30-40.

1
2
3
4
5
6
7
8
9
10
11
12

CBI

(a)
(b)
(c)
(d)
(e)
(f)
(g)
(h)
(i)
(j)
(k)



A.2

Total no. of balls = No. of red balls + No. of black balls
 = 4 + 6

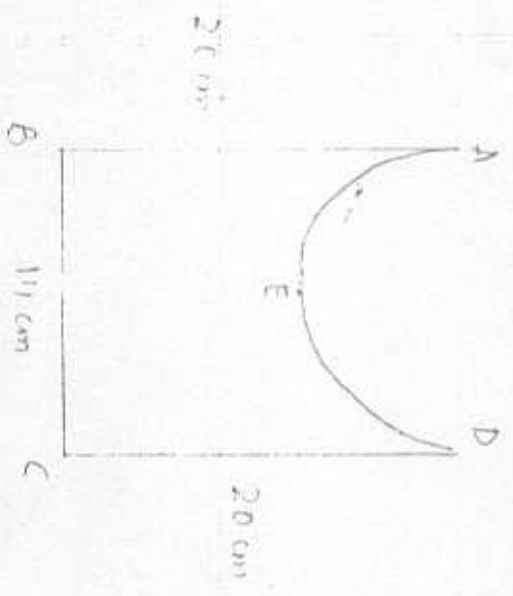
= 10

No. of black balls = 6

$$P(\text{black ball}) = \frac{\text{No. of black balls}}{\text{Total no. of balls}} = \frac{6}{10} = \frac{3}{5}$$

$$P(\text{black ball}) = \frac{3}{5}$$

A.3



For rectangle ABCD,

length = L = 20 cm

breadth = b = 14 cm

For semicircle AED,

diameter = breadth of rectangle

$$= d = 14 \text{ cm}$$

Perimeter of figure = $AB + BC + CD + \text{length of arc } \widehat{AED}$

M-3

$$= 20 + 14 + 20 + (\pi r)$$

$$= 54 + 22 \times \frac{7}{7}$$

$$= 76 \text{ cm.}$$

$$\text{Perimeter} = \boxed{76 \text{ cm.}}$$

$$\text{A.4} \quad \sin 3\theta = \cos(\theta - 6^\circ)$$

$$\Rightarrow \cos(90^\circ - 3\theta) = \cos(\theta - 6^\circ)$$

$$[\because \sin \theta = \cos(90^\circ - \theta)]$$

$$\Rightarrow 90^\circ - 3\theta = \theta - 6^\circ$$

$$\Rightarrow 4\theta = 96^\circ$$

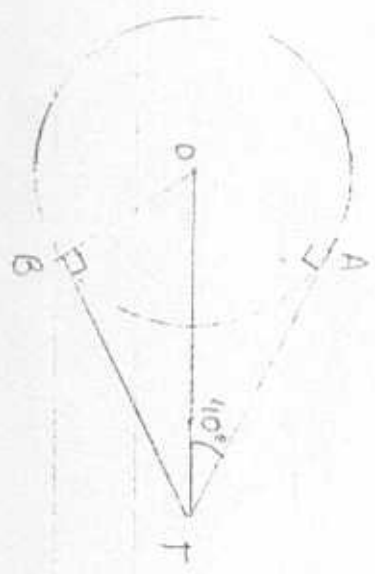
$$\Rightarrow \theta = 24^\circ$$

$$\therefore \theta = \boxed{24^\circ}$$

CBSE :

- 1.
 - 2.
 - 3.
 - 4.
 - 5.
 - 6.
 - 7.
 - 8.
 - 9.
 - 10.
 - 11.
 - 12.
- (a) (b) (c) (d) (e) (f) (g) (h) (i) (j) (k) (l) (m) (n) (o) (p) (q) (r) (s) (t) (u) (v) (w) (x) (y) (z)

A.5



Given : In $\angle (O, OA)$, $\angle ATO = 40^\circ$.

To find : $\angle AOB$.

Solution : AT and BT are tangents to $\angle (O, OA)$.

$\Rightarrow AT = BT$ [Tangents from an external point are equal] - (1)

In $\Delta s AOT$ and BOT

$AT = BT$ [From (1)]

$AO = OB$ [Radii]

$OT = TO$ [Common]

$\therefore \Delta AOT \cong \Delta BOT$ [SSS congruency]

$\Rightarrow \angle AOT = \angle BOT$ and - (2)

$\angle ATO = \angle BTO$ - (3)

⇒ ∠BTO = ∠ATO = 40° [From (3)].

In ΔBTO,

∠OBT = 90° [∵ Tangent is ⊥ to radius through point of contact]. —(4).

∠BOT + ∠OTB + ∠OBT = 180° [Angle Sum Property of Δ].

⇒ ∠BOT + 40° + 90° = 180° [From (3), (4)].

⇒ ∠BOT = 180° - 130°

⇒ ∠BOT = 50°.

∠AOT = ∠BOT = 50° [From (2)]. — (5).

∠AOB = ∠AOT + ∠BOT

= 50° + 50° [From (5)].

= 100°

∴ ∠AOB = 100°

CBSE

- 1. 3
- 2. 3
- 3. 3
- 4. 3
- 5. 3
- 6. 3
- 7. 3
- 8. 3
- 9. 3
- 10. 3
- 11. 3
- 12. 3
- (1)
- (2)
- (3)
- (4)
- (5)
- (6)
- (7)
- (8)
- (9)
- (10)
- (11)
- (12)



A.6

$$\sqrt{2} = 1.414 \dots \text{ (approx)}$$

$$\sqrt{3} = 1.732 \dots \text{ (approx)}$$

∴ Rational no. between $\sqrt{2}$ and $\sqrt{3}$ is ~~15~~ ~~16~~ $= \frac{16}{15} = \frac{8}{5}$

Required rational no. between $\sqrt{2}$ and $\sqrt{3}$ is $\frac{8}{5}$ or 1.6

A.7

Since the graph of $y = f(x)$ intersects the x -axis at 3 points, No. of zeroes of polynomial $y = f(x)$ is $\boxed{3}$

A.8

$$2x^2 + 5x - 12 = 0$$

$$\text{L.H.S.} \therefore 2(-4)^2 + 5(-4) - 12$$

$$= 2(16) + (-20) - 12$$

$$= 32 - 20 - 12$$

$$= 32 - 32$$

$$= 0$$

$$\text{R.H.S.} = 0$$

∴ since ~~LHS = RHS = 0~~

$\Rightarrow x = -4$ satisfies the equation $2x^2 + 5x - 12 = 0$.

$\therefore x = -4$ is a solution of the equation $2x^2 + 5x - 12 = 0$.

A 9

AP is $\sqrt{8}, \sqrt{18}, \sqrt{32}, \dots$

This is the same as $2\sqrt{2}, 3\sqrt{2}, 4\sqrt{2}, \dots$

Here

first term = $a_1 = 2\sqrt{2}$

common difference = $a_2 - a_1 = d = 3\sqrt{2} - 2\sqrt{2} = \sqrt{2}$

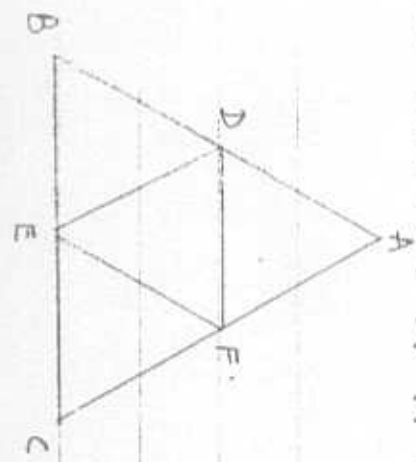
$a_2 =$ second term = $3\sqrt{2}$

$a_3 =$ third term = $4\sqrt{2}$

$a_4 =$ fourth term = $a_3 + d = 4\sqrt{2} + \sqrt{2} = 5\sqrt{2} = \sqrt{50}$

\therefore Next term of the AP is $\sqrt{50}$

A.10



Given : In $\triangle ABC$, D, F and E are the mid-points of AB, AC and BC respectively.

To find : an $\triangle DEF$
in $\triangle ABC$.

Solution : Since D and F are mid-points of AB and AC,

$$\Rightarrow DF = \frac{1}{2} BC$$

[Mid-point theorem]

$$\Rightarrow \frac{DF}{BC} = \frac{1}{2}$$

-(1)

Similarly, $\frac{EF}{AB} = \frac{1}{2}$

-(2)

$$\text{Also, } \frac{DE}{AC} = \frac{1}{2}$$

-(3)

From (1), (2), (3),

In Δ s DEF and ABC.

$$\frac{DE}{BC} = \frac{EF}{AB} = \frac{DF}{AC} = \frac{1}{2}$$

$\therefore \Delta DEF \sim \Delta CAB$ [SSS similarity].

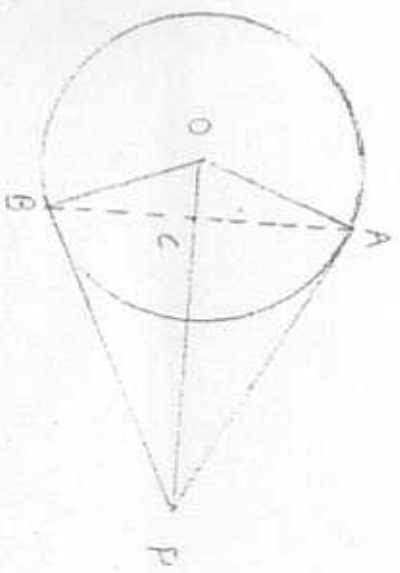
$\frac{\text{Area } \Delta DEF}{\text{Area } \Delta CAB} = \left(\frac{DE}{BC}\right)^2$ [Ratios of areas of two similar Δ s is equal to the square of the ratio of their corresponding sides].

$$\Rightarrow \frac{\text{Area } \Delta DEF}{\text{Area } \Delta CAB} = \left(\frac{1}{2}\right)^2$$

$$\therefore \frac{\text{Area } \Delta DEF}{\text{Area } \Delta ABC} = \frac{1}{4}$$

SECTION - B

A.11



Given : In $c(O, OA)$, $OP =$ diameter of circle.

To prove : $\triangle ABP$ is equilateral.

Construction : Join AB . Intersecting OP at C .

Proof : Here, $OP \subset$ diameter of $c(O, OA)$.

$$\Rightarrow OP = 2 \times \text{radius}$$

$$\Rightarrow OP = 2OA$$

$$\Rightarrow \frac{OP}{OA} = \frac{2}{1} \quad \text{--- (1)}$$

Also, $\angle OAP = \angle OBP = 90^\circ$ [Given].

→ No. of ... For first ... For second ... For third ... For fourth ... For fifth ... For sixth ... For seventh ... For eighth ... For ninth ... For tenth ...

In right ΔOAP ,

$$\frac{OP}{AO} = \frac{2}{7}$$

[From (1)]

$$\Rightarrow \frac{AO}{OP} = \frac{1}{2}$$

$$\Rightarrow \sin P = \frac{1}{2}$$

$$\Rightarrow \sin P = \sin 30^\circ$$

$$\Rightarrow P = 30^\circ$$

$$\Rightarrow \angle APO = 30^\circ$$

--- (2)

In ΔAOP and BOP ,

$$BO = AO$$

[radii]

$$\angle OAP = \angle OBP = 90^\circ$$

[given]

$$OP = OP$$

[common]

$$\therefore \Delta AOP \cong \Delta BOP$$

[RHS congruency]

$$\Rightarrow \angle AOP = \angle BOP$$

[cpct]

--- (3)

- 1. 3
- 2. 4
- 3. 31
- 4. 5
- 5. 31
- 6. 31
- 7. 31
- 8. 31
- 9. 31
- 10. 31
- 11. 31
- 12. 31

$\Rightarrow \angle BPD = \angle APD = 30^\circ$ [From (2)] - (4)

Also, In ΔAOP ,

$\angle AOP + \angle OPA + \angle PAO = 180^\circ$ [Angle sum property of a Δ]

$\Rightarrow \angle AOP + 30^\circ + 90^\circ = 180^\circ$ [From (4)]

$\Rightarrow \angle AOP = 180^\circ - 120^\circ$

$\Rightarrow \angle AOP = 60^\circ$ - (5)

In ΔAOC and ΔOCB ,

$\angle AOC = \angle BOC$ [From (3)]

$AO = BO$ [Radii]

$OC = CO$ [Common]

$\therefore \Delta AOC \cong \Delta BOC$ [SAS congruency]

$\Rightarrow \angle OAC = \angle OBC$ - (6)

$\angle OCA = \angle OCB$ - (7)

$\angle AOC + \angle OCB = 180^\circ$ [Linear pair]

$\Rightarrow 2\angle AOC = 180^\circ$ [From (7)]

$\Rightarrow \angle AOC = 90^\circ$ - (8)

In ΔAOC ,

$$\angle AOC + \angle ACO + \angle CAO = 180^\circ \quad \text{[Angle sum property of a } \Delta \text{].}$$

$$\Rightarrow 60^\circ + 90^\circ + \angle CAO = 180^\circ \quad \text{[From (5), (8)].}$$

$$\Rightarrow \angle CAO = 180^\circ - 150^\circ$$

$$\Rightarrow \angle OAC = 30^\circ \quad \text{--- (9).}$$

Also, $\angle OAP = 90^\circ$ [Given].

$$\Rightarrow \angle OAC + \angle CAP = 90^\circ$$

$$\Rightarrow 30^\circ + \angle CAP = 90^\circ$$

$$\Rightarrow \angle CAP = 60^\circ \quad \text{--- (10).}$$

Since $\angle OAC = 30^\circ$

$$\Rightarrow \angle OOC = \angle OAC = 30^\circ \quad \text{[From (6)].}$$

$$\Rightarrow \angle POC = 60^\circ \quad \text{--- (11).}$$

$$\angle APB = \angle APO + \angle BPO$$

$$= 30^\circ + 30^\circ \quad \text{[From (4)].}$$

$$= 60^\circ \quad \text{[Given]}$$

$$\Rightarrow \angle APB = 60^\circ \quad \text{--- (12).}$$

From (10), (11) and (12),

In ΔAPB ,

$$\angle PBA = \angle CAP = \angle APB = 60^\circ$$

$\therefore \Delta APB$ is an equilateral Δ [\because All angles are 60° each].

Hence proved.

A.12.

$$ax^2 - 6x - 6 = p(x)$$

Product of zeroes = 4.

Also,

Product of zeroes = $\frac{\text{constant term}}{\text{coefficient of } x^2}$

$$\Rightarrow 4 = \frac{-6}{a}$$

$$\Rightarrow a = \frac{-6}{4}$$

$$\Rightarrow n = -2$$

$$\boxed{n = -2}$$

A.13

For what value of k are the points ...

$$A(1, 1) \quad x_1 = 1 \quad y_1 = 1$$

$$B(3, k) \quad x_2 = 3 \quad y_2 = k$$

$$C(-1, 4) \quad x_3 = -1 \quad y_3 = 4$$

Since

if A, B and C are collinear.

$$\Rightarrow \text{Ar } ABC = 0$$

$$\Rightarrow \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] = 0$$

$$\Rightarrow \frac{1}{2} [(1)(k-4) + 3(4-1) + (-1)(1-k)] = 0$$

$$\Rightarrow k-4 + 9 - 1 + k = 0$$

$$\Rightarrow 2k + 9 - 5 = 0$$

$$\Rightarrow 2k + 4 = 0$$

$$\Rightarrow k = -\frac{4}{2}$$

 \therefore

$$k = -2$$

- 1. 30
- 2. 30
- 3. 30
- 4. 30
- 5. 30
- 6. 30
- 7. 30
- 8. 30
- 9. 30
- 10. 30
- 11. 30
- 12. 30
- (a)
- (b)
- (c)
- (d)
- (e)
- (f)
- (g)
- (h)
- (i)
- (j)
- (k)
- (l)
- (m)
- (n)
- (o)
- (p)
- (q)
- (r)
- (s)
- (t)
- (u)
- (v)
- (w)
- (x)
- (y)
- (z)

A.14

(i)

Total no. of cards = $50 - 5 + 1 = 46$.
 No. of cards with a prime no. less than 10
 = 2 i.e. 5 and 7.

P (prime no. less than 10) = $\frac{\text{No. of cards with a prime no. less than 10}}{\text{Total no. of cards}}$

$$= \frac{2}{46} = \frac{1}{23}$$

(ii)

No. of cards with a perfect square no. = 5 (i.e. 9, 16, 25, 36, 49).
 P (perfect square no.) = $\frac{\text{No. of cards with a perfect square no.}}{\text{Total no. of cards}}$

$$= \frac{5}{46}$$

(i) P (prime no. less than 10) =

$$\frac{1}{23}$$

(ii) P (perfect square no.) =

$$\frac{5}{46}$$

A.15

$$7 \sin^2 \theta + 3 \cos^2 \theta = 4$$

$$\Rightarrow 7 \sin^2 \theta + 3(1 - \sin^2 \theta) = 4$$

$$[\because \sin^2 \theta + \cos^2 \theta = 1]$$

$$\Rightarrow \cos^2 \theta = 1 - \sin^2 \theta$$

$$\Rightarrow 7 \sin^2 \theta + 3 - 3 \sin^2 \theta = 4$$

$$\Rightarrow 4 \sin^2 \theta = 1$$

$$\Rightarrow \sin^2 \theta = \frac{1}{4}$$

$$\Rightarrow \sin \theta = \sqrt{\frac{1}{4}}$$

$$\Rightarrow \sin \theta = \frac{1}{2}$$

— (1)

$$\cos \theta = \sqrt{1 - \sin^2 \theta}$$

$$= \sqrt{1 - \left(\frac{1}{2}\right)^2}$$

$$= \sqrt{1 - \frac{1}{4}}$$

$$= \sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{2}$$

— (2)

$$[\because \sin^2 \theta + \cos^2 \theta = 1]$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta} = \frac{\frac{1}{2}}{\frac{\sqrt{3}}{2}} = \frac{1}{\sqrt{3}}$$

[From (1), (2)]

$$\boxed{\tan \theta = 1}$$

Hence proved.

A-16

~~By Euclid's division lemma~~Let a be any positive integer. Then,

By Euclid's division lemma,

i.e. $a = bq + r$ $0 \leq r < b$. a can be of the form $3q$, $3q+1$ or $3q+2$ where q is some inCase I: $a = 3q$.

$$a^2 = (3q)^2 = 9q^2 = 3(3q^2) = 3m \text{ where } m = 3q^2 \quad \text{---(1)}$$

Case II: $a = 3q+1$.

$$\begin{aligned} a^2 &= (3q+1)^2 = 9q^2 + 6q + 1 \\ &= 3(3q^2 + 2q) + 1 \\ &= 3m + 1 \text{ where } m = 3q^2 + 2q. \end{aligned} \quad \text{---(2)}$$

Case III: $a = 3q+2$.

$$\begin{aligned} a^2 &= (3q+2)^2 = 9q^2 + 12q + 4 \\ &= 3(3q^2 + 4q + 1) + 1. \end{aligned} \quad \text{[} \because (a+b)^2 = a^2 + 2ab + b^2 \text{]}$$

CBSE

1. 10
2. 10
3. 10
4. 10
5. 10
6. 10
7. 10
8. 10
9. 10
10. 10
11. 10
12. 10

$$= 3m + 1 \quad \text{where } m = 3q^2 + 4q + 1 \quad \text{--- (3)}$$

From (1), (2) and (3),

We conclude,

The square of any positive integer is of the form $3m$ or $3m+1$ for some integer m .

Hence proved.

A.17

$$37x + 43y = 123 \quad \text{--- (1)}$$

$$43x + 37y = 117 \quad \text{--- (2)}$$

Adding (1) and (2),

$$37x + 43y = 123$$

$$43x + 37y = 117$$

$$\hline 80x + 80y = 240$$

$$\Rightarrow 80(x+y) = 80(3)$$

$$\Rightarrow x+y = 3$$

--- (3)

From (1) and (3)

~~$$37x + 43(3-x) = 123$$~~

$$37x + 43y = 123$$

$$\begin{array}{r} (-) \\ 43x + 37y = 117 \\ (-) \end{array}$$

$$-6x + 6y = 6.$$

$$\Rightarrow -6(x-y) = -6(-1)$$

$$\Rightarrow x-y = -1.$$

Adding (3) and (4),

$$x+y = 3$$

$$x-y = -1.$$

$$2x = 2.$$

$$\Rightarrow x = 1.$$

Substituting $x = 1$ in (4),

$$1-y = -1.$$

$$\Rightarrow -y = -2.$$

$$\Rightarrow y = 2.$$

$$\therefore \boxed{x=1} \quad \boxed{y=2}$$

A18

Let us assume, to the contrary that $\sqrt{5}$ is rational. Then,

$\sqrt{5} = \frac{a}{b}$, where a and b are positive coprime integers and $b \neq 0$

$$\Rightarrow a = \sqrt{5}b$$

$$\Rightarrow a^2 = 5b^2 \quad \text{[Squaring both sides]} \quad \dots (1)$$

$$\Rightarrow 5 \text{ divides } 5b^2$$

$$\Rightarrow 5 \text{ divides } a^2 \quad \text{[}\because a^2 = 5b^2\text{]}$$

$\Rightarrow 5$ divides a \therefore If p divides a^2 then p divides a $\dots (2)$

$\Rightarrow a = 5c$ for some integer c .

$$\Rightarrow a^2 = 25c^2 \quad \text{[Squaring both sides]}$$

$$\Rightarrow 5b^2 = 25c^2 \quad \text{[From (1)]}$$

$$\Rightarrow b^2 = 5c^2 \quad \dots (3)$$

$$\Rightarrow 5 \text{ divides } 5c^2$$

$$\Rightarrow 5 \text{ divides } b^2 \quad \text{[From (3), } b^2 = 5c^2\text{]}$$

$$\Rightarrow 5 \text{ divides } b$$

From (2) and (4), \therefore If p divides a^2 , then p divides a $\dots (4)$

$\therefore 5$ is a common factor of a and b

- 1. उत्तर
- 2. उत्तर
- 3. उत्तर
- 4. उत्तर
- 5. उत्तर
- 6. उत्तर
- 7. उत्तर
- 8. उत्तर
- 9. उत्तर
- 10. उत्तर
- 11. उत्तर
- 12. उत्तर

But this contradicts the fact that a and b are coprime
i.e. they have no common factor apart from 1.

This means our assumption is wrong.

$\sqrt{5}$ is an irrational no. Hence proved.

A.19

Let the AP be $a_1, a_2, a_3, a_4, \dots$ where

first term = a

common difference = d .

Then,

$$a_n = a + (n-1)d.$$

$$\Rightarrow a_4 = a + (4-1)d$$

$$\Rightarrow a_4 = a + 3d.$$

$$a_2 = a + (2-1)d$$

$$\Rightarrow a_2 = a + d.$$

$$a_6 = a + (6-1)d$$

$$\Rightarrow a_6 = a + 5d.$$

$$a_{10} = a + (10-1)d$$

-(1)

-(2)

~~-(2)~~

-(3)

Also,

$$a_4 + a_8 = 24.$$

$$\Rightarrow a + 3d + a + 7d = 24$$

[From (1), (2)]

$$\Rightarrow 2a + 10d = 24.$$

$$\Rightarrow a + 5d = 12.$$

-(5)

$$a_6 + a_{10} = 44.$$

$$\Rightarrow a + 5d + a + 9d = 44$$

[From (3), (4)]

$$\Rightarrow 2a + 14d = 44$$

$$\Rightarrow a + 7d = 22$$

-(6)

Subtracting (5) from (6),

$$a + 7d = 22$$

$$a + 5d = 12$$

$$\hline 2d = 10.$$

$$\Rightarrow d = 5$$

Substituting $d = 5$ in (5),

$$a + 5(5) = 12.$$

$$\Rightarrow a + 25 = 12.$$

$$\Rightarrow a = -13.$$

$$a_1 = -13$$

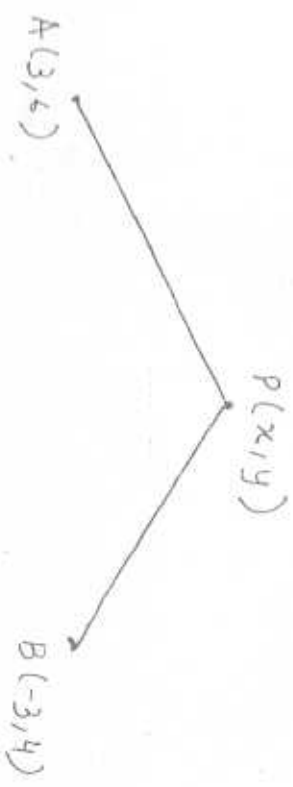
$$a_2 = a_1 + d = -13 + 5 = -8.$$

$$a_3 = a_2 + d = -8 + 5 = -3.$$

First three terms of the AP are $\boxed{-13, -8 \text{ and } -3}$.

~~A-20~~

A 20



Here.

$A(3, 6) \quad x_1 = 3 \quad y_1 = 6$

$B(-3, 4) \quad x_2 = -3 \quad y_2 = 4$

$P(x, y)$

According to Problem,

P is equidistant from A and B .

$\Rightarrow AP = BP$

$\Rightarrow AP^2 = BP^2$

By distance formula,

distance between two points = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Now,

$AP^2 = PB^2$

$\Rightarrow (x_1 - x)^2 + (y_1 - y)^2 = (x_2 - x)^2 + (y_2 - y)^2$

$\Rightarrow (3 - x)^2 + (6 - y)^2 = (-3 - x)^2 + (4 - y)^2$

[Distance formula]

1. 3
2. 3
3. 3
4. 3
5. 3
6. 3
7. 3
8. 3
9. 3
10. 3
11. 3
12. 3

$$\Rightarrow x^2 - 6x + 36 + y^2 - 12y = x^2 + 6x + 16 + y^2 - 8y$$

$$\Rightarrow -12y + 8y - 6x - 6x + 36 - 16 = 0$$

$$\Rightarrow -4y - 12x + 20 = 0$$

$$\Rightarrow -12x - 4y + 20 = 0$$

$$\Rightarrow -4(3x + y - 5) = -4(0)$$

$$\Rightarrow 3x + y - 5 = 0$$

$$\boxed{3x + y - 5 = 0}$$

Hence proved.

A.21

To prove: $(\sin\theta + \operatorname{cosec}\theta)^2 + (\cos\theta + \operatorname{sec}\theta)^2 = 7 + \tan^2\theta + \cot^2\theta$.

$$\text{LHS} = (\sin\theta + \operatorname{cosec}\theta)^2 + (\cos\theta + \operatorname{sec}\theta)^2$$

$$= \sin^2\theta + \operatorname{cosec}^2\theta + 2\sin\theta \operatorname{cosec}\theta + \cos^2\theta + \operatorname{sec}^2\theta + 2\cos\theta \operatorname{sec}\theta$$

$$[\because (a+b)^2 = a^2 + 2ab + b^2]$$

$$= \sin^2\theta + \cos^2\theta + \operatorname{cosec}^2\theta + \operatorname{sec}^2\theta + 2\sin\theta \left(\frac{1}{\sin\theta}\right) + 2\cos\theta \left(\frac{1}{\cos\theta}\right)$$

$$[\because \operatorname{cosec}\theta = \frac{1}{\sin\theta}, \operatorname{sec}\theta = \frac{1}{\cos\theta}]$$

$$= 1 + \cancel{\cos^2\theta} + \cancel{\sec^2\theta} + 2 + 2$$

$$= 5 + \cancel{\cos^2\theta} + \cancel{\sec^2\theta}$$

$$= 5 + 1 + \cancel{\cot^2\theta} + 1 + \cancel{\tan^2\theta}$$

$$= 7 + \cancel{\tan^2\theta} + \cancel{\cot^2\theta}$$

$$= \text{R.H.S.}$$

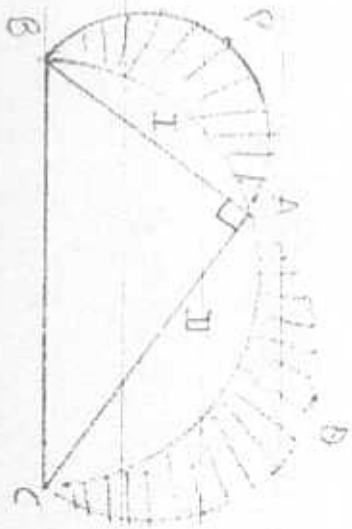
Since LHS = RHS.

Hence verified.

$$\because \cos^2\theta - \cot^2\theta = 1$$

$$\sec^2\theta - \tan^2\theta = 1$$

A.22



In $\triangle ABC$, right angled at A,

$$AB^2 + AC^2 = BC^2$$

[Pythagoras Theorem]

$$\Rightarrow 3^2 + 4^2 = BC^2$$

$$\Rightarrow BC^2 = 9 + 16$$

$$\Rightarrow BC^2 = 25$$

$$\Rightarrow BC = 5 \text{ units}$$

$$\Rightarrow \text{Diameter of semicircle } BAC = BC = 5 \text{ units} = d$$

$$\text{Radius} = \frac{d}{2} = \frac{5}{2} \text{ units}$$

$$\begin{aligned} \text{Area of semicircle } BAC &= \frac{\pi r^2}{2} = \left(\frac{22}{7} \times \frac{5}{2} \times \frac{5}{2} \right) \times \frac{1}{2} \text{ units}^2 \quad \text{--- (1)} \end{aligned}$$

Diameter of semicircle $\widehat{APB} = AB = 3$ units = d .

radius = $r_1 = \frac{d}{2} = \frac{3}{2}$ units.

Area of semicircle $\widehat{APB} = \frac{\pi r_1^2}{2} = \left(\frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} \times \frac{1}{2} \right)$ units²

Diameter of semicircle $\widehat{ADC} = AC = 4$ units = d_2 .

radius = $r_2 = \frac{d_2}{2} = \frac{4}{2} = 2$ units.

Area of semicircle $\widehat{ADC} = \frac{\pi r_2^2}{2} = \left(\frac{22}{7} \times 2 \times 2 \times \frac{1}{2} \right)$ units² = (3)

~~Area of shaded region~~

Area of $\triangle ABC = \frac{1}{2} \times \text{base} \times \text{height} = \frac{1}{2} \times 4 \times 3 = 6$ units²

Area of shaded region = Area of semicircle \widehat{APB} + Area of semicircle \widehat{ADC} - (Area of $\triangle ABC$)

= $\frac{1}{2} \times \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} + \frac{1}{2} \times \frac{22}{7} \times 2 \times 2 \times \frac{1}{2} - \left(\frac{1}{2} \times 4 \times 3 \right) + 6$

1
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11
12
CBSI

$$\begin{aligned}
 &= \left(\frac{1}{2} \times \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} + \frac{1}{2} \times \frac{22}{7} \times 2 \times 2 \times \frac{1}{2} - \frac{1}{2} \times \frac{22}{7} \times \frac{5}{2} \times \frac{5}{2} \right) + 6 \\
 &= \frac{1}{2} \times \frac{22}{7} \times \left(\frac{3}{2} \times \frac{3}{2} + 2 \times 2 - \frac{5}{2} \times \frac{5}{2} \right) + 6 \\
 &= \frac{11}{7} \left(\frac{9}{4} + 4 - \frac{25}{4} \right)
 \end{aligned}$$

Area of I + II = Area of semicircle \widehat{AC} - Area of $\triangle ABC$.

$$= \frac{1}{2} \times \frac{22}{7} \times \frac{5}{2} \times \frac{5}{2} - 6. \quad [\text{From (1) \& (4)}].$$

$$= \frac{275}{28} - \frac{168}{28}$$

$$= \frac{107}{28} \text{ units}^2 \quad \text{--- (5)}$$

Area of shaded region = Area of semicircle \widehat{AB} + Area of semicircle \widehat{AC}

- Area of I + II.

$$= \frac{1}{2} \times \frac{22}{7} \times \frac{3}{2} \times \frac{3}{2} + \frac{1}{2} \times \frac{22}{7} \times \frac{5}{2} \times \frac{5}{2} - \left(\frac{107}{28} \right) \quad [\text{From (2), (3), (5)}].$$

Qc

275
168
107
28
4.75
6
10.75

$$= \frac{1}{2} \times \frac{24}{7} \times \frac{1}{2} \times \frac{1}{2} (9 + 16) - \frac{107}{28}$$

$$= \frac{11 \times 25 - 107}{28}$$

$$= \frac{275 - 107}{28}$$

$$= \frac{168}{28}$$

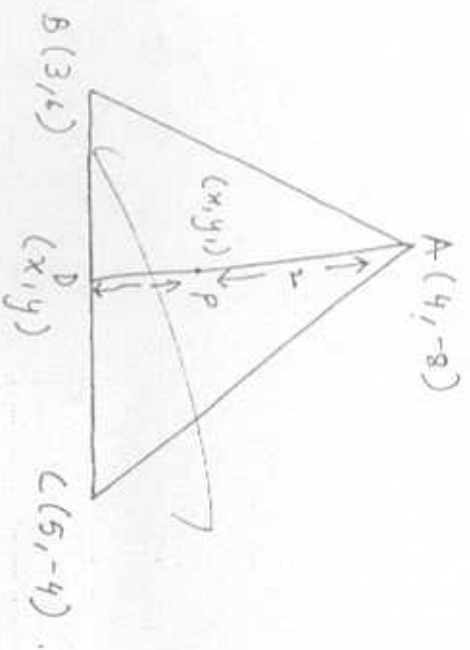
$$= \frac{24}{4}$$

$$= 6 \text{ units}^2$$

Area of shaded region is  6 sq. units

1. 5
 2. 1
 3. 3
 4. 3
 5. 3
 6. 3
 7. 3
 8. 3
 9. 3
 10. 3
 11. 3
 12. 3
- CBS
- (क) 3
 (ख) 3
 (ग) 3
 (घ) 3
 (ङ) 3
 (च) 3
 (छ) 3
 (ज) 3

A. 23



Here in $\triangle ABC$.

$$A(4, -8)$$

$$B(3, 6)$$

$$C(5, -4)$$

D is mid-point of BC .

By mid pt. formula, $x = \frac{x_1 + x_2}{2}$, $y = \frac{y_1 + y_2}{2}$.

$$\Rightarrow x = \frac{3 + 5}{2}, \quad y = \frac{6 + (-4)}{2}$$

$$\Rightarrow x = 4, \quad y = 1$$

∴ Coordinates of D are $D(4, 1)$.

Now,

$$\frac{AP}{PD} = \frac{2}{1}$$

Let $AP = m$ and $PD = n$.

$$\frac{(4, -8)}{A} \leftarrow 2 \rightarrow P \leftarrow 1 \cdot \frac{(x, y)}{D}$$

By section formula, $x = \frac{m x_2 + n x_1}{m+n}$, $y = \frac{m y_2 + n y_1}{m+n}$.

$$\Rightarrow x_1 = \frac{2(4) + 1(4)}{2+1}, \quad y_1 = \frac{2(1) + 1(-8)}{2+1}$$

$$\Rightarrow x_1 = \frac{8+4}{3}, \quad y_1 = \frac{2-8}{3}$$

$$\Rightarrow x_1 = \frac{12}{3}, \quad y_1 = \frac{-6}{3}$$

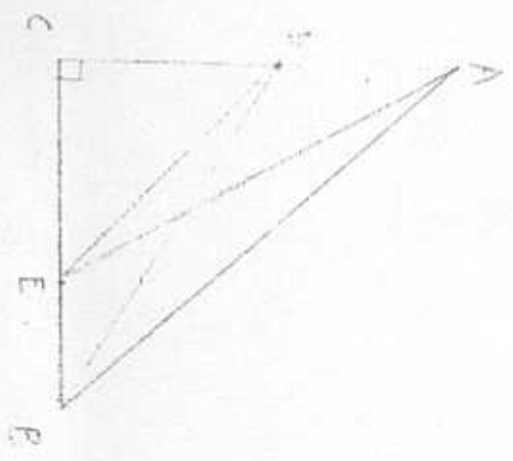
$$\Rightarrow x_1 = 4, \quad y_1 = -2.$$

∴ Coordinates of P are $P(4, -2)$.

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11. उत्तर
12. उत्तर

A.8.4.

4.11)



Given : In $\triangle ABC$, $\angle ACB = 90^\circ$, D and E are points on AC and BC respectively.

To prove : $AE^2 + BD^2 = AB^2 + DE^2$.

Construction : Join DE, AE and BD.

Proof : By Pythagoras Theorem,

In $\triangle ACB$,

$$AC^2 + CB^2 = AB^2 \quad \text{--- (1)}$$

In $\triangle DCE$,

$$DC^2 + CE^2 = DE^2 \quad \text{--- (2)}$$

In $\triangle DCB$,

$$DC^2 + CB^2 = DB^2$$

-(3)

In $\triangle ACE$,

$$AC^2 + CE^2 = AE^2$$

-(4)

Adding (1) and (2),

$$AB^2 + DE^2 = AC^2 + BC^2 + DC^2 + CE^2$$

$$= (AC^2 + CE^2) + (BC^2 + DC^2)$$

$$= AE^2 + BD^2$$

$$\therefore AB^2 + DE^2 = AE^2 + BD^2$$

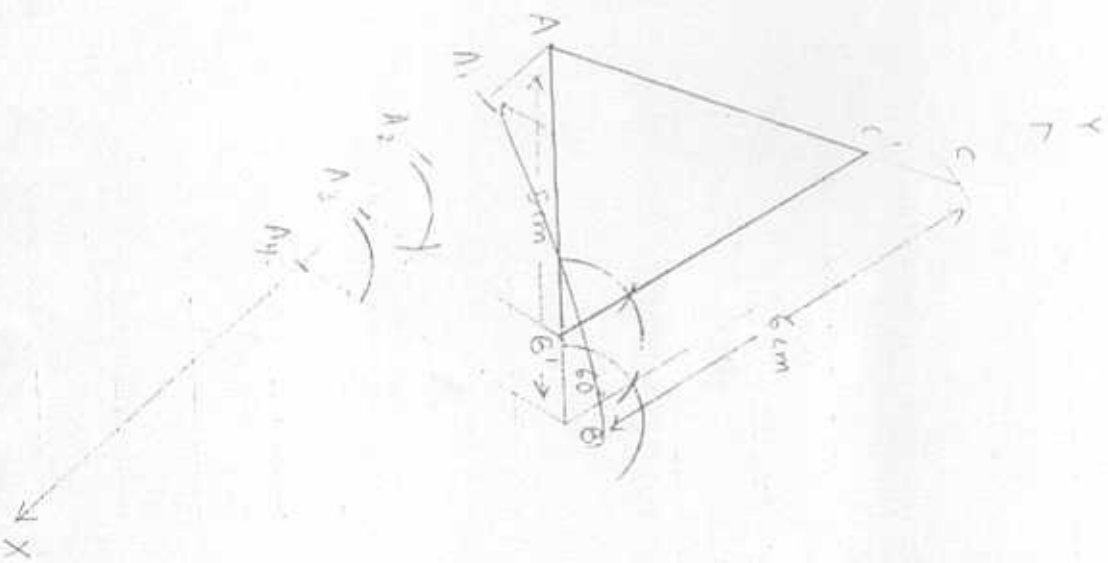
Hence proved.

[Rearranging terms]
[From (3), (4)]

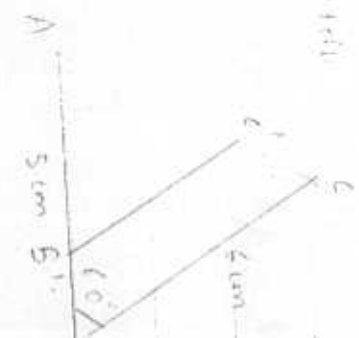
CBS

1. 1
2. 2
3. 3
4. 3
5. 3
6. 3
7. 3
8. 3
9. 3
10. 3
11. 3
12. 3

A 25.



rough sketch



M-36

$\Delta AB'C'$ is the required Δ

$$\frac{AB'}{AB} = \frac{B'C'}{BC} = \frac{A'C'}{AC} = \frac{3}{4}$$

$\Delta ABC \sim \Delta AB'C'$

In ΔABC ,

$AB = 5 \text{ cm}$

~~$BC = 6 \text{ cm}$~~

$\angle ABC = 60^\circ$

A-26

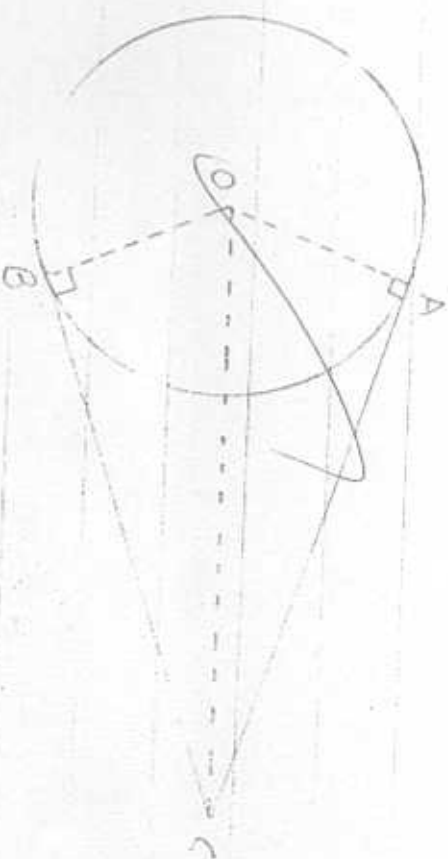
SECTION-D

M-37

Given: In $c(O, OA)$, AC and BC are tangents to the circle from point C.
To prove: $AC = BC$.

Construction: Join OA, OB and OC.

Figure:



Proof: In Δs AOB and BOC

$$AO = OB$$

$$OC = CO$$

[Radii of same circle]
[Common]

$$\angle OAC = \angle OBC = 90^\circ$$

[\therefore Tangent is \perp to radius through point of contact]

$$\Rightarrow \Delta AOC \cong \Delta BOC$$

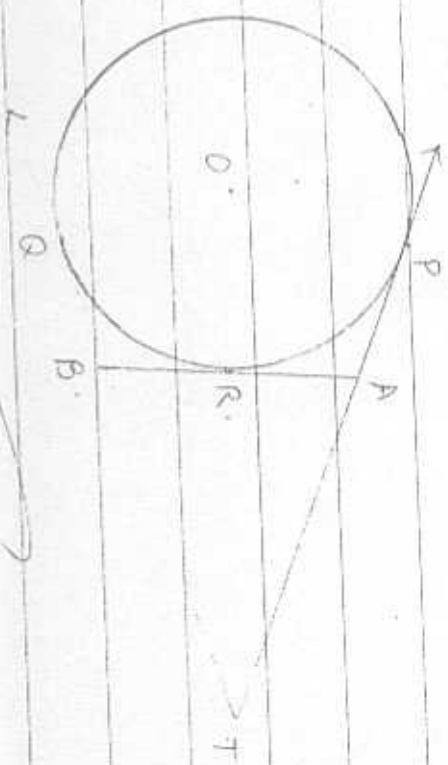
$$\Rightarrow AC = BC$$

[RHS congruency]
[C.P.T.]

$$\therefore AC = BC$$

Hence proved.

Ruler:



Given : In $\odot (O, OP)$, PT and AT are tangents from P to circle. R is a point on the circle, AB is a tangent to the circle at R .

To prove : $TA + AR = TB + BR$.

Proof : Since tangents from an external point are equal.

$\Rightarrow PT = QT$ -(1)

$AP = AR$ -(2)

$BR = BQ$ -(3)

Now,

$PT = QT$ [From (1)]

$\Rightarrow PA + AT = QB + BT$

$\Rightarrow AR + AT = BR + BT$ [From (2), (3)]

$TA + AR = TR + BR$

A-27

M-39

Let the time taken by smaller pipe to fill the tank separately be x hrs.
 Then time taken by larger pipe to fill tank separately = $(x-10)$ hrs.

Part of tank filled by small pipe in x hrs = 1.

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Part of tank filled by large pipe in $(x-10)$ hrs = 1.

$$1 \text{ hr} = \frac{1}{x-10} \quad \text{--- (1)}$$

$$9 \frac{3}{8} \text{ hrs} = \frac{75}{8(x-10)} \quad \text{--- (2)}$$

A to B,

$$\frac{75}{8x} + \frac{75}{8(x-10)} = 1.$$

$$\Rightarrow \frac{75}{8} \left(\frac{x-10}{2x} + \frac{1}{x-10} \right) = 1.$$

$$\Rightarrow \frac{1}{x} + \frac{1}{x-10} = \frac{8}{75}$$

$$\Rightarrow \frac{x-10+x}{x(x-10)} = \frac{8}{75}$$

$$\Rightarrow \frac{2x-10}{x^2-10x} = \frac{8}{75}$$

$$\Rightarrow 150x - 750 = 8x^2 - 10x \cdot 8$$

$$\Rightarrow 8x^2 - 10x - 150x + 750 = 0$$

$$\Rightarrow 8x^2 - 140x + 750 = 0$$

$$\Rightarrow 4x^2 - 70x + 375 = 0$$

\Rightarrow

$$\Rightarrow \frac{x-18 \pm x}{x(x-10)} = \frac{8}{75}$$

$$\Rightarrow \frac{2x-10}{x^2-10x} = \frac{8}{75}$$

$$\Rightarrow 150x - 750 = 8x^2 - 80x$$

$$\Rightarrow 8x^2 - 230x + 750 = 0$$



$$\Rightarrow 4x^2 - 11$$

$$\Rightarrow 4x^2 - 100x - 15x + 375 = 0$$

$$\Rightarrow 4x(x - 25) - 15(x - 25) = 0$$

$$\Rightarrow (4x - 15)(x - 25) = 0$$

$$\Rightarrow (4x - 15) = 0 \quad \text{or} \quad x - 25 = 0$$

$$\Rightarrow x = \frac{15}{4} \quad \text{or} \quad x = 25$$

When $x = \frac{15}{4}$,

$$x - 10 = \frac{15}{4} - \frac{40}{4} = \frac{25}{4}$$

Time cannot be ~~we~~

3322
 0
 150
 150
 325
 125
 5
 2
 3325

25
 13
 12

$\Rightarrow x = \frac{15}{4}$ is not possible.

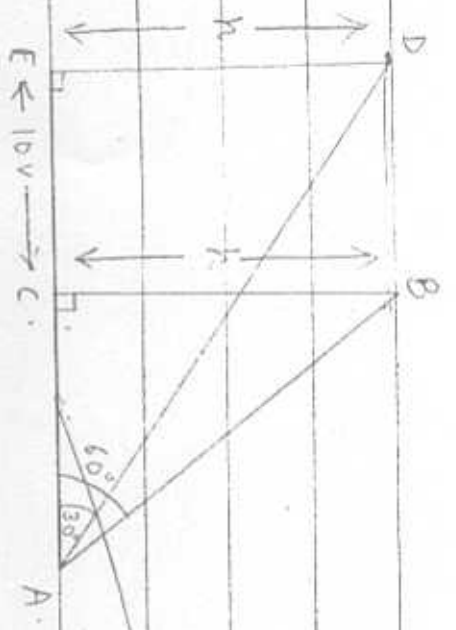
$\Rightarrow x = 25$ hrs.

$$x - 10 = 25 - 10 = 15 \text{ hrs}$$

\therefore Time taken by small pipe is ~~95 hrs~~ and that taken by larger pipe is 25 hrs.

\therefore Time taken by small pipe is 95 hrs and time taken by larger pipe is 15 hrs

A. 88



let the jet originally be at B and let C be the ground. Then,

A is the point of observation

$$\Rightarrow \angle BAC = 60^\circ.$$

let the new position of jet be D. Then

$$\angle DAE = 30^\circ.$$

let the height at which the jet is flying be h m above ground.

let speed of the jet be v m/s. Then,

$$t = 10s.$$

$$\text{distance} = \cancel{10v} = 10v \cdot \cancel{m} = CE \quad \text{--- (1)}$$

ΔA

In ΔBAC , right angled at C,

$$\tan 60^\circ = \frac{BC}{AC}$$

$$\Rightarrow \sqrt{3} = \frac{h}{AC}$$

$$\Rightarrow h = \sqrt{3} AC \quad \text{---(1)}$$

In ΔDAE , right angled at E,

$$\tan 30^\circ = \frac{DE}{AE}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{h}{AC + CE}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{\sqrt{3} AC}{AC + 10}$$

[From (1) & (2)]

$$\Rightarrow AC + 10 = 3 AC$$

$$\Rightarrow 2AC = 10V$$

$$\Rightarrow AC = 5V$$

Substituting $AC = 5V$ in (1),

$$h = \sqrt{3} (5V)$$

$$= 5\sqrt{3} V$$

(3)

Speed = ~~648 km/hr.~~

~~$$\frac{648}{1000} \div \frac{1}{3600} \text{ m/s}$$~~

~~$$\frac{648}{1000} \times 3600 \text{ m/s}$$~~

~~$$= \frac{648}{5000}$$~~

~~$$\times \frac{18}{3600}$$~~

~~$$= 2304 \text{ m/s}$$~~

648

64
36
2304
648
18
3600
648
18
3600
648
18
3600

Speed = 648 km/hr

⇒ v = $\frac{648000}{3600}$ m/s.

⇒ v = $\frac{1080}{6}$

⇒ v = 180 m/s.

Substituting v = 180 m/s in

h = 1.5√3 v

= 5√3 × 180

= 900√3

= 900 × 1.732

= 1558.80 m. = 1.5588 km

The jet is flying at a constant height of 1558.80 m

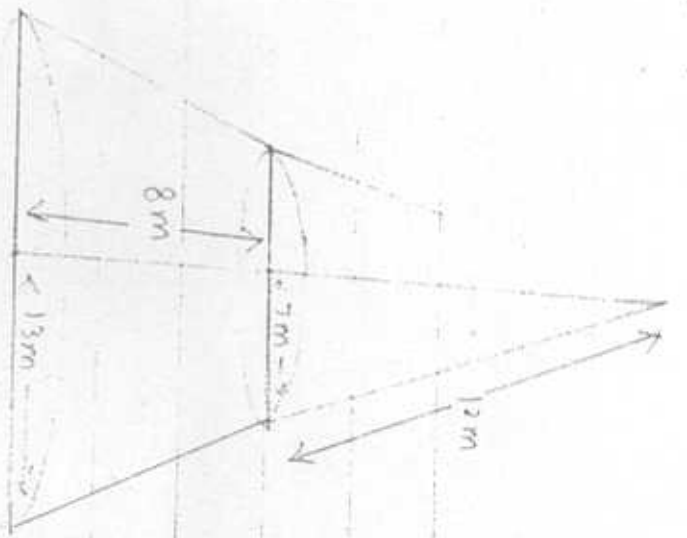
or 1.5588 km

$\frac{648}{36}$

$\frac{61732}{1558.800}$

$\frac{61732}{9}$
 $\frac{1558.800}{9}$

A.29



For frustum,

$$\text{diameter}_1 = d_1 = 26 \text{ m}$$

$$\text{radius}_1 = r_1 = \frac{d_1}{2} = 13 \text{ m}$$

$$\text{diameter}_2 = d_2 = 14 \text{ m}$$

$$\text{radius}_2 = r_2 = \frac{d_2}{2} = 7 \text{ m}$$

$$\text{height} = h = 8 \text{ m}$$

$$\begin{aligned}
 \text{Slant height} = l &= \sqrt{h^2 + (r_1 - r_2)^2} \\
 &= \sqrt{8^2 + (13 - 7)^2} \\
 &= \sqrt{64 + 36} \\
 &= \sqrt{100} \\
 &= 10 \text{ cm}
 \end{aligned}$$

For cone,

$$\text{diameter} = d_2 = 14 \text{ m}$$

$$\text{radius} = r_2 = 7 \text{ m}$$

$$\text{Slant height} = l_1 = 12 \text{ m}$$

Area of ~~surface~~ curved surface required = Curved surface Area of frustum + Curved

$$\text{Surface Area of cone} = \pi (r_1 + r_2) l + \pi r_2 l_1$$

$$= \pi [(13 + 7)(12) + (7)(12)]$$

$$= \pi [200 + 84]$$

$$= \frac{22}{7} \times 284$$



$$= \frac{22}{7} \times 284$$

$$= 6248$$

$$\frac{6248}{7}$$

$$= \frac{892 \times 7}{4} = 892.571$$

$$= 892.71 \text{ m}^2 = 892.57$$

∴ Area of canvas required is 892.71 m^2

∴ Area of canvas required is 892.57 m^2

$$\begin{array}{r} 126 \\ \times 5 \\ \hline 630 \\ \times 1 \\ \hline 126 \\ \hline 630 \end{array}$$

$$\begin{array}{r} 18284 \\ \times 3 \\ \hline 54852 \\ \times 18 \\ \hline 329112 \\ \hline 62492 \end{array}$$

M-50

Class Intervals	f_i	x_i	$u_i = \frac{x_i - a}{h}$	$f_i u_i$	cf
0-10	3	5	-3	-9	3
10-20	4	15	-2	-8	7
20-30	7	25	-1	-7	14
30-40	15	35 = a	0	0	29
40-50	10	45	1	10	39
50-60	7	55	2	14	46
60-70	4	65	3	12	50
	$\sum_{i=1}^n f_i = 50$			$\sum_{i=1}^n f_i u_i = 12$	

Let assumed mean be $a = 35$.

Width of class intervals = $h = 10$.

$$\bar{x} = a + \frac{\sum_{i=1}^n f_i u_i}{\sum_{i=1}^n f_i} \times h$$

$$= 35 + \frac{12}{50} \times 10$$

M-51

$$= 35 + 2.4$$

$$= 37.4.$$

$$\therefore \text{Mean} = 37.4.$$

$$\text{No. of observations} = N = 50 \quad \frac{N}{2} = 25.$$

$$\text{Median class} = 30-40.$$

$$\text{Lower limit of median class} = l = 30.$$

$$\text{Cumulative frequency of class preceding median class} = 14 = cf$$

$$\text{Frequency of median class} = 15 = f$$

$$\text{Width of class intervals} = h = 10.$$

$$\text{Median} = l + \frac{\frac{N}{2} - cf}{f} \times h$$

$$= 30 + \frac{25 - 14}{15} \times 10 = 30 + \frac{11 \times 2}{3} = 30 + \frac{22}{3}$$

$$= 30 + 7.33 = 37.33$$

\therefore Median = 37.33.

Modal class = 30-40.

Lower limit of modal class = $L = 30$.

Frequency of modal class = $f_1 = 15$.

Frequency of class preceding modal class = $f_0 = 7$.

Frequency of class succeeding modal class = $f_2 = 10$.

Width of class intervals = $h = 10$.

Mode = $L + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h$

~~$= 30 + \frac{15 - 7}{30 - 7 - 10} \times 10$~~

$= 30 + \frac{80}{13}$

$$= 36.15$$

$$\therefore \text{Mode} = 36.15.$$

Mean = 37.4
Median = 37.33
Mode = 36.15.

M-83