

**DESIGN OF QUESTION PAPER**

**MATHEMATICS**

**CLASS XII**

**Time : 3 Hours**

**Max. Marks : 100**

Weightage of marks over different dimensions of the question paper shall be as follows:

**A. Weightage to different topics/content units**

S.No.	Topics	Marks
1.	Relations and Functions	10
2.	Algebra	13
3.	Calculus	44
4.	Vectors & three-dimensional Geometry	17
5.	Linear programming	06
6.	Probability	10
	<b>Total</b>	<b>100</b>

**B. Weightage to different forms of questions**

S.No.	Forms of Questions	Marks for each question	No. of Questions	Total marks
1.	Very Short Answer questions (VSA)	01	10	10
2.	Short Answer questions (SA)	04	12	48
3.	Long answer questions (LA)	06	07	42
	<b>Total</b>		<b>29</b>	<b>100</b>

**C. Scheme of Options**

There will be no overall choice. However, an internal choice in any four questions of four marks each and any two questions of six marks each has been provided.

**D. Difficulty level of questions**

S.No.	Estimated difficulty level	Percentage of marks
1.	Easy	15
2.	Average	70
3.	Difficult	15

Based on the above design, separate sample papers along with their blue prints and Marking schemes have been included in this document. About 20% weightage has been assigned to questions testing higher order thinking skills of learners.

**CBSE SAMPLE PAPER - I**  
**CLASS XII MATHEMATICS**  
**BLUE PRINT - I & II**

S. No.	Topics	VSA	SA	LA	Total
1. (a)	Relations and Functions	1(1)	4(1)	-	
(b)	Inverse Trigonometric Functions	1(1)	4(1)	-	10(4)
2. (a)	Matrices	2(2)	-	6(1)	
(b)	Determinants	1(1)	4(1)	-	13(5)
3. (a)	Continuity and differentiability	-	8(2)	-	
(b)	Applications of derivatives	-	4(1)	6(1)	
(c)	Integration	2(2)	4(1)	6(1)	
(d)	Application of Integrals	-	-	6(1)	
(e)	Differential Equations	-	8(2)	-	44(11)
4. (a)	Vectors	2(2)	4(1)	-	
(b)	3-dimensional Geometry	1(1)	4(1)	6(1)	17(6)
5.	Linear - Programming	-	-	6(1)	6(1)
6.	Probability	-	4(1)	6(1)	10(2)
	Total	10(10)	48(12)	42(7)	100(29)

**SAMPLE PAPER - I**

**MATHEMATICS**

**CLASS - XII**

**Time : 3 Hours**

**Max. Marks : 100**

**General Instructions**

1. All questions are compulsory.
2. The question paper consist of 29 questions divided into three sections A, B and C. Section A comprises of 10 questions of one mark each, section B comprises of 12 questions of four marks each and section C comprises of 07 questions of six marks each.
3. All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
4. There is no overall choice. However, internal choice has been provided in 04 questions of four marks each and 02 questions of six marks each. You have to attempt only one of the alternatives in all such questions.
5. Use of calculators in not permitted. You may ask for logarithmic tables, if required.

### SECTION A

1. Give an example to show that the relation R in the set of natural numbers, defined by  $R = \{(x, y), x, y \in \mathbb{N}, x \leq y^2\}$  is not transitive.
2. Write the principal value of  $\cos^{-1}(\cos \frac{5\pi}{3})$ .
3. Find x, if  $\begin{pmatrix} 5 & 3x \\ 2y & z \end{pmatrix} = \begin{pmatrix} 5 & 4 \\ 12 & 6 \end{pmatrix}^T$ .
4. For what value of a,  $\begin{pmatrix} 2a & -1 \\ -8 & 3 \end{pmatrix}$  is a singular matrix?
5. A square matrix A, of order 3, has  $|A| = 5$ , find  $|A \cdot \text{adj}A|$ .
6. Evaluate  $\int 5^x dx$
7. Write the value of  $\int_{-\pi/2}^{\pi/2} \sin^2 x dx$ .
8. Find the position vector of the midpoint of the line segment joining the points  $A(5\hat{i} + 3\hat{j})$  and  $B(3\hat{i} - \hat{j})$ .
9. If  $\vec{a} = 2\hat{i} - \hat{j} + 3\hat{k}$  and  $\vec{b} = (6\hat{i} + \lambda\hat{j} + 9\hat{k})$  and  $\vec{a} \parallel \vec{b}$ , find the value of  $\lambda$ .
10. Find the distance of the point (a,b,c) from x-axis.

### SECTION B

11. Let N be the set of all natural numbers and R be the relation in  $\mathbb{N} \times \mathbb{N}$  defined by (a,b) R (c,d) if  $ad=bc$ . Show that R is an equivalence relation.
12. Prove that  $\tan^{-1}\left(\frac{1}{4}\right) + \tan^{-1}\left(\frac{2}{9}\right) = \frac{1}{2} \cos^{-1}\left(\frac{3}{5}\right)$ .

OR

Solve for x :  $\sin^{-1}(1-x) - 2\sin^{-1}x = \frac{\pi}{2}$ .

13. Using properties of determinants, prove that :

$$\begin{vmatrix} a^2+1 & ab & ac \\ ab & b^2+1 & bc \\ ca & cb & c^2+1 \end{vmatrix} = (1+a^2+b^2+c^2).$$

14. For what values of a and b, the function f defined as :

$$f(x) = \begin{cases} 3ax+b, & \text{if } x < 1 \\ 11, & \text{if } x = 1 \\ 5ax-2b, & \text{if } x > 1 \end{cases} \text{ is continuous at } x=1$$

15. If  $x^y + y^x = a^b$ , find  $\frac{dy}{dx}$ .

OR

If  $x = a(\cos t + t \sin t)$  and  $y = b(\sin t - t \cos t)$ , find  $\frac{d^2y}{dx^2}$ .

16. Find the intervals in which the following function is strictly increasing or strictly decreasing

$$f(x) = 20 - 9x + 6x^2 - x^3$$

OR

For the curve  $y = 4x^3 - 2x^5$ , find all points at which the tangent passes through origin.

17. Evaluate :  $\int \frac{\sin x + \cos x}{\sqrt{\sin x \cdot \cos x}} dx$

OR

$$\text{Evaluate : } \int e^x \left( \frac{x^2+1}{(x+1)^2} \right) dx$$

18. Form the differential equation of the family of circles having radii 3.

19. Solve the following differential equation:

$$\sqrt{1+x^2+y^2+x^2y^2} + xy \frac{dy}{dx} = 0.$$

20. If the sum of two unit vectors is a unit vector, show that the magnitude of their difference is  $\sqrt{3}$ .

21. Find whether the lines  $\vec{r} = (\hat{i} - \hat{j} - \hat{k}) + \lambda (2\hat{i} + \hat{j})$  and  $\vec{r} = (2\hat{i} - \hat{j}) + \mu(\hat{i} + \hat{j} - \hat{k})$  intersect or not. If intersecting, find their point of intersection.
22. Three balls are drawn one by one without replacement from a bag containing 5 white and 4 green balls. Find the probability distribution of number of green balls drawn.

### SECTION C

23. If  $A = \begin{pmatrix} 2 & 1 & 3 \\ 4 & -1 & 0 \\ -7 & 2 & 1 \end{pmatrix}$ , find  $A^{-1}$  and hence solve the following system of equations :

$$2x + y + 3z = 3$$

$$4x - y = 3$$

$$-7x + 2y + z = 2$$

OR

Using elementary transformations, find the inverse of the matrix :

$$\begin{pmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{pmatrix}$$

24. If the length of three sides of a trapezium, other than the base are equal to 10cm each, then find the area of trapezium when it is maximum.
25. Draw a rough sketch of the region enclosed between the circles  $x^2 + y^2 = 4$  and  $(x-2)^2 + y^2 = 1$ . Using integration, find the area of the enclosed region.
26. Evaluate  $\int_1^2 (x^2 + x + 2) dx$  as a limit of sums.

OR

Evaluate  $\int_0^1 \sin^{-1}(x\sqrt{1-x} - \sqrt{x}\sqrt{1-x^2}) dx, 0 \leq x \leq 1$

27. Find the coordinates of the foot of the perpendicular and the perpendicular distance of the point (1, 3, 4) from the plane  $2x - y + z + 3 = 0$ . Find also, the image of the point in the plane.
28. An aeroplane can carry a maximum of 200 passengers. A profit of Rs. 1000 is made on each executive class ticket and a profit of Rs. 600 is made on each economy class ticket. The airline reserves at least 20 seats for the executive class. However, at least 4 times as many passengers prefer to travel by economy class, than by the executive class. Determine how many tickets of each type must be sold, in order to maximise profit for the airline. What is the maximum profit? Make an L.P.P. and solve it graphically.

29. A fair die is rolled. If 1 turns up, a ball is picked up at random from bag A, if 2 or 3 turns up, a ball is picked up at random from bag B, otherwise a ball is picked up from bag C. Bag A contains 3 red and 2 white balls, bag B contains 3 red and 4 white balls and bag C contains 4 red and 5 white balls. The die is rolled, a bag is picked up and a ball is drawn from it. If the ball drawn is red, what is the probability that bag B was picked up?

**MARKING SCHEME**  
**MATHEMATICS CLASS - XII**  
**SAMPLE PAPER 1**

**SECTION A**

1.  $(8, 3) \in R, (3, 2) \in R$  but  $(8, 2) \notin R$ .

2.  $\frac{\pi}{3}$

3.  $x = 4$

4.  $a = \frac{4}{3}$

5. 125

6.  $\frac{5^x}{\log 5} + c$

7. Zero.

8.  $4\hat{i} + \hat{j}$

9.  $\lambda = -3$

10.  $\sqrt{b^2 + c^2}$

(1 mark for correct answer for Qs. 1 to 10)

**SECTION B**

11. For any  $(a, b) \in N \times N, ab = ba$   
 $\Rightarrow (a, b) R (a, b)$ . Thus R is reflexive. 1

Let  $(a, b) R (c, d)$  for any  $a, b, c, d \in N$

$\therefore ad = bc$

$\Rightarrow cb = da \Rightarrow (c, d) R (a, b)$

$\therefore R$  is symmetric 1

Let  $(a, b) R (c, d)$  and  $(c, d) R (e, f)$  for  $a, b, c, d, e, f \in N$

then  $ad = bc$  and  $cf = de$

$\Rightarrow adcf = bcde$  or  $af = be \Rightarrow (a, b) R (e, f)$

$\therefore R$  is transitive 1½

Since, R is reflexive, symmetric and transitive, hence R is an equivalence relation. ½



$$12. \text{ L.H.S} = \tan^{-1} \left( \frac{\frac{1}{4} + \frac{2}{9}}{1 - \frac{1}{4} \cdot \frac{2}{9}} \right) = \tan^{-1} \left( \frac{17}{34} \right) = \tan^{-1} \left( \frac{1}{2} \right) \quad 1\frac{1}{2}$$

$$= \frac{1}{2} \left( 2 \tan^{-1} \left( \frac{1}{2} \right) \right) = \frac{1}{2} \cos^{-1} \left[ \frac{1 - \left( \frac{1}{2} \right)^2}{1 + \left( \frac{1}{2} \right)^2} \right] \quad 1\frac{1}{2}$$

$$= \frac{1}{2} \cos^{-1} \left( \frac{1 - \frac{1}{4}}{1 + \frac{1}{4}} \right) = \frac{1}{2} \cos^{-1} \frac{3}{5} = \text{RHS} \quad 1$$

OR

$$\sin^{-1}(1-x) - 2\sin^{-1}x = \frac{\pi}{2} \Rightarrow \sin^{-1}(1-x) = \frac{\pi}{2} + 2\sin^{-1}x \quad \frac{1}{2}$$

$$\Rightarrow (1-x) = \sin\left(\frac{\pi}{2} + 2\sin^{-1}x\right) = \cos(2\sin^{-1}x) \quad \frac{1}{2}$$

$$\Rightarrow (1-x) = \cos(2\alpha) \text{ where } \sin^{-1}x = \alpha \text{ or } x = \sin\alpha \quad \frac{1}{2}$$

$$\Rightarrow (1-x) = 1 - 2\sin^2\alpha = 1 - 2x^2, \therefore 2x^2 - x = 0 \quad 1$$

$$\Rightarrow x(2x-1) = 0 \quad \frac{1}{2}$$

$$\therefore x = 0, \frac{1}{2}$$

Since  $x = \frac{1}{2}$  does not satisfy the given equation  $\therefore x=0$

$$13. \text{ LHS} = \frac{1}{abc} \begin{vmatrix} a(a^2+1) & a^2b & a^2c \\ ab^2 & b(b^2+1) & b^2c \\ ac^2 & bc^2 & c(c^2+1) \end{vmatrix} = \frac{abc}{abc} \begin{vmatrix} a^2+1 & a^2 & a^2 \\ b^2 & b^2+1 & b^2 \\ c^2 & c^2 & c^2+1 \end{vmatrix} \quad 1$$

$$R_1 \rightarrow R_1 + R_2 + R_3 = \begin{vmatrix} 1+a^2+b^2+c^2 & 1+a^2+b^2+c^2 & 1+a^2+b^2+c^2 \\ b^2 & b^2+1 & b^2 \\ c^2 & c^2 & c^2+1 \end{vmatrix} \quad 1$$

$$= (1+a^2+b^2+c^2) \begin{vmatrix} 1 & 1 & 1 \\ b^2 & b^2+1 & b^2 \\ c^2 & c^2 & c^2+1 \end{vmatrix} = (1+a^2+b^2+c^2) \begin{vmatrix} 1 & 0 & 0 \\ b^2 & 1 & 0 \\ c^2 & 0 & 1 \end{vmatrix} \quad 1$$

$$= (1+a^2+b^2+c^2) \cdot 1 = (1+a^2+b^2+c^2) \quad 1$$

14.  $\lim_{x \rightarrow 1^-} f(x) = 3a+b$ , RHL =  $\lim_{x \rightarrow 1^+} f(x) = 5a-2a$ ,  $f(1) = 11$  2

$$\therefore 3a+b = 11, \quad 5a-2b = 11 \quad 1$$

Solving to get  $a = 3, b = 2$  1

15. Put  $x^y = u$  and  $y^x = v \therefore u+v = a^b \Rightarrow \frac{du}{dx} + \frac{dv}{dx} = 0$   $\frac{1}{2}$

$$\log u = y \log x \Rightarrow \frac{1}{u} \frac{du}{dx} = \frac{y}{x} + \log x \cdot \frac{dy}{dx} \therefore \frac{du}{dx} = y \cdot x^{y-1} + x^y \cdot \log x \cdot \frac{dy}{dx} \quad 1$$

$$\log v = x \log y \Rightarrow \frac{1}{v} \frac{dv}{dx} = \frac{x}{y} \frac{dy}{dx} + \log y \therefore \frac{dv}{dx} = xy^{x-1} \cdot \frac{dy}{dx} + y^x \cdot \log y \quad 1$$

$$\therefore y \cdot x^{y-1} + x^y \log x \frac{dy}{dx} + xy^{x-1} \frac{dy}{dx} + y^x \log y = 0 \quad 1$$

$$\Rightarrow \frac{dy}{dx} = - \frac{y \cdot x^{y-1} + y^x \cdot \log y}{x^y \cdot \log x + x y^{x-1}} \quad \frac{1}{2}$$

OR

$$\frac{dx}{dt} = a(-\sin t + t \cos t + \sin t) = at \cos t \quad 1$$

$$\frac{dy}{dt} = b(\cos t + t \sin t - \cos t) = bt \sin t \quad 1$$

$$\therefore \frac{dy}{dx} = \frac{b}{a} \cdot \tan t \Rightarrow \frac{d^2y}{dx^2} = \frac{b}{a} \sec^2 t \cdot \frac{dt}{dx} \quad 1$$

$$\therefore \frac{d^2y}{dx^2} = \frac{b}{a} \sec^2 t \cdot \frac{1}{at \cos t} = \frac{b \sec^3 t}{a^2 t} \quad 1$$

16.  $f'(x) = 0 \Rightarrow -9+12x-3x^2 = 0 \Rightarrow -(3)(x-1)(x-3) = 0$  1

$$\therefore x = 1, x = 3$$

$\therefore$  The intervals are  $(-\infty, 1), (1, 3), (3, \infty)$  1

Getting  $f(x)$  to be strictly decreasing in  $(-\infty, 1) \cup (3, \infty)$  1

and strictly increasing in  $(1, 3)$  1

OR

Let  $(x_1, y_1)$  be a point on the given curve, the tangent at which passes through origin.

$$\therefore \text{Slope of tangent} = \frac{y_1}{x_1} \quad \text{----- (i)} \quad \frac{1}{2}$$

$$\text{also, } \frac{dy}{dx} = 12x^2 - 10x^4 \Rightarrow \text{slope of tangent} = 12x_1^2 - 10x_1^4 \quad \text{----- (ii)} \quad \frac{1}{2}$$

$$\Rightarrow \frac{y_1}{x_1} = 12x_1^2 - 10x_1^4 \text{ or } y_1 = 12x_1^3 - 10x_1^5 \Rightarrow 4x_1^3 - 2x_1^5 = 12x_1^3 - 10x_1^5 \quad 1$$

$$\text{solving to get } x_1 = 0 \text{ or } 1 - x_1^2 = 0 \text{ i.e. } x_1 = \pm 1 \quad 1$$

Hence the required points are  $(0, 0)$ ,  $(1, 2)$  and  $(-1, -2)$  1

17. Putting  $(\sin x - \cos x) = t$  to get  $(\cos x + \sin x) dx = dt$  1

$$\text{and } \sin^2 x + \cos^2 x - 2\sin x \cos x = t^2 \text{ or } \sin x \cos x = \frac{1}{2} (1 - t^2) \quad \frac{1}{2}$$

$$\therefore \text{Given integral} = \sqrt{2} \int \frac{dt}{\sqrt{1-t^2}} = \sqrt{2} \cdot \sin^{-1} t + c \quad 1\frac{1}{2}$$

$$= \sqrt{2} \sin^{-1} (\sin x - \cos x) + c \quad 1$$

OR

$$\int e^x \cdot \frac{x^2+1}{(x+1)^2} dx = \int e^x \cdot \frac{[(x^2+1)^2 - 2x]}{(x+1)^2} dx \quad 1$$

$$= \int e^x dx - 2 \int e^x \cdot \frac{(x+1-1)}{(x+1)^2} dx \quad 1$$

$$= e^x - 2 \int \left[ \frac{1}{x+1} - \frac{1}{(x+1)^2} \right] e^x dx \quad 1$$

$$= e^x - 2 \cdot \frac{e^x}{x+1} + c \quad [\text{using } \int e^x (f(x) + f'(x)) dx = e^x f(x) + c] \quad 1$$

18. The equation of the family of circles is  $(x-a)^2 + (y-b)^2 = 9$  -----(i) 1/2

$$\Rightarrow 2(x-a) + 2(y-b) \frac{dy}{dx} = 0 \text{ or } (x-a) = -(y-b) \frac{dy}{dx} \quad \text{-----(ii)} \quad 1$$

$$\Rightarrow 1+(y-b)\frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 0 \Rightarrow (y-b) = -\frac{\left[1+\left(\frac{dy}{dx}\right)^2\right]}{\frac{d^2y}{dx^2}} \text{-----(iii)} \quad 1$$

$$\text{from (ii), } (x-a) = +\frac{\left[1+\left(\frac{dy}{dx}\right)^2\right]}{\frac{d^2y}{dx^2}} \cdot \frac{dy}{dx} \quad \frac{1}{2}$$

$$\text{putting in (i) to get } \left[\frac{1+\left(\frac{dy}{dx}\right)^2}{\frac{d^2y}{dx^2}}\right]^2 \left(\frac{dy}{dx}\right)^2 + \left[\frac{1+\left(\frac{dy}{dx}\right)^2}{\frac{d^2y}{dx^2}}\right]^2 = 9 \quad \frac{1}{2}$$

$$\text{or } \left[\frac{1+\left(\frac{dy}{dx}\right)^2}{\frac{d^2y}{dx^2}}\right]^2 \left[\left(\frac{dy}{dx}\right)^2 + 1\right] = 9 \Rightarrow \left[1+\left(\frac{dy}{dx}\right)^2\right]^3 = 9\left(\frac{d^2y}{dx^2}\right)^2 \quad \frac{1}{2}$$

19. Given differential equation can be written as

$$\sqrt{(1+x^2)(1+y^2)} + xy \frac{dy}{dx} = 0 \quad \frac{1}{2}$$

$$\Rightarrow \frac{\sqrt{1+x^2}}{x} dx + \frac{y}{\sqrt{1+y^2}} dy = 0 \quad \frac{1}{2}$$

$$\therefore \int \frac{y}{\sqrt{1+y^2}} dy = -\int \frac{\sqrt{1+x^2}}{x^2} x dx \quad \frac{1}{2}$$

Putting  $1+y^2 = u^2$  and  $1+x^2 = v^2$  to get  $y dy = u du$  and  $x dx = v dv$  1/2

$$\therefore \int \frac{u du}{u} = -\int \frac{v \cdot v dv}{v^2-1} = -\int \frac{v^2-1+1}{v^2-1} dv = \int \left(1 + \frac{1}{v^2-1}\right) dv \quad 1$$

$$u = -v \cdot \frac{1}{2} \log \left| \frac{v-1}{v+1} \right| + c \text{ or } \sqrt{1+y^2} = -\sqrt{1+x^2} - \frac{1}{2} \log \left| \frac{\sqrt{1+x^2}-1}{\sqrt{1+x^2}+1} \right| + c \quad 1$$

20. Let  $\hat{a}$ ,  $\hat{b}$  and  $\hat{c}$  be unit vector such that  $\hat{a} + \hat{b} = \hat{c}$  1
- $\therefore |\hat{a} + \hat{b}| = 1 \Rightarrow 1 = |\hat{a} + \hat{b}|^2 = \hat{a}^2 + \hat{b}^2 + 2\hat{a} \cdot \hat{b} = 2 + 2\hat{a} \cdot \hat{b}$  1
- $\Rightarrow 2(\hat{a} \cdot \hat{b}) = 1 - 2 = -1$  -----(i) 1/2
- Now  $|\hat{a} - \hat{b}|^2 = \hat{a}^2 + \hat{b}^2 - 2\hat{a} \cdot \hat{b} = 1 + 1 - (-1) = 3$  1 1/2
- $\Rightarrow |\hat{a} - \hat{b}| = \sqrt{3}$  1/2

21. Given lines are  $\vec{r} = (1+2\lambda)\hat{i} + (-1+\lambda)\hat{j} - \hat{k}$  and 1/2
- $\vec{r} = (2+\mu)\hat{i} + (-1+\mu)\hat{j} - \mu\hat{k}$  1/2

If lines are intersecting, then for some value of  $\lambda$  and  $\mu$ ,

$1 + 2\lambda = 2 + \mu$ , --(i)  $-1 + \lambda = -1 + \mu$  --(ii)  $-1 = -\mu$  --(iii) 1

Solving (ii) and (iii) to get  $\lambda = 1$ ,  $\mu = 1$ , which satisfy (i) hence the line are intersecting 1

and point of intersection is  $(3, 0, -1)$

22. Let X denotes the random variable, 'number of green balls,
- |        |                     |                                |                                |                     |   |
|--------|---------------------|--------------------------------|--------------------------------|---------------------|---|
| X :    | 0                   | 1                              | 2                              | 3                   | 1 |
| P(X) : | $\frac{5c_3}{9c_3}$ | $\frac{5c_2 \cdot 4c_1}{9c_3}$ | $\frac{5c_1 \cdot 4c_1}{9c_3}$ | $\frac{4c_3}{9c_3}$ | 1 |
|        | $= \frac{5}{42}$    | $\frac{10}{21}$                | $\frac{5}{14}$                 | $\frac{1}{21}$      | 2 |

### SECTION C

23.  $|A| = 2(-1) - 1(4) + 3(1) = -3 \neq 0$   $A^{-1} = \frac{1}{|A|} \text{adj } A$  1
- The cofactors are 2
- $A_{11} = -1, A_{12} = -4, A_{13} = 1$
- $A_{21} = 5, A_{22} = 23, A_{23} = -11$
- $A_{31} = 3, A_{32} = 12, A_{33} = -6$
- $\therefore A^{-1} = -\frac{1}{3} \begin{pmatrix} -1 & 5 & 3 \\ -4 & 23 & 12 \\ 1 & -11 & -6 \end{pmatrix}$  1/2

Given equations can be written as

$$\begin{pmatrix} 2 & 1 & 3 \\ 4 & -1 & 0 \\ -7 & 2 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 3 \\ 3 \\ 2 \end{pmatrix} \text{ or } A \cdot X = B$$

$$\therefore X = A^{-1} \cdot B$$

$$\therefore \begin{pmatrix} x \\ y \\ z \end{pmatrix} = -\frac{1}{3} \begin{pmatrix} -1 & 5 & 3 \\ -4 & 23 & 12 \\ 1 & -11 & -6 \end{pmatrix} \begin{pmatrix} 3 \\ 3 \\ 2 \end{pmatrix} = \begin{pmatrix} -6 \\ -27 \\ 14 \end{pmatrix}$$

$$\therefore x = -6, y = -27, z = 14$$

OR

$$\text{Let } A = \begin{pmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{pmatrix} \text{ then } \begin{pmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 3 & -2 & 4 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} A$$

$$R_3 \rightarrow R_3 - 3R_1 \Rightarrow \begin{pmatrix} 1 & -1 & 2 \\ 0 & 2 & -3 \\ 0 & +1 & -2 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ -3 & 0 & 1 \end{pmatrix} A$$

$$R_2 \leftrightarrow R_3 \Rightarrow \begin{pmatrix} 1 & -1 & 2 \\ 0 & 1 & -2 \\ 0 & 2 & -3 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ -3 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} A$$

$$R_3 \rightarrow R_3 - 2R_2 \Rightarrow \begin{pmatrix} 1 & -1 & 2 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ -3 & 0 & 1 \\ 6 & 1 & -2 \end{pmatrix} A$$

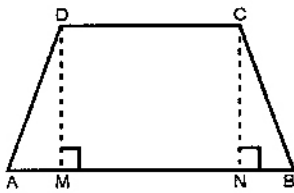
$$R_1 \rightarrow R_1 + R_2 \Rightarrow \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} -2 & 0 & 1 \\ -3 & 0 & 1 \\ 6 & 1 & -2 \end{pmatrix} A$$

$$R_2 \rightarrow R_2 + 2R_3 \Rightarrow \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} -2 & 0 & 1 \\ 9 & 2 & -3 \\ 6 & 1 & -2 \end{pmatrix} A$$

$$\text{Hence } A^{-1} = \begin{pmatrix} -2 & 0 & 1 \\ 9 & 2 & -3 \\ 6 & 1 & -2 \end{pmatrix}$$

1/2

24.



$$AD = DC = BC = 10 \text{ cm.}$$

$$\Delta ADM \cong \Delta BCN \therefore AM = BN = x \text{ (say)}$$

$$\therefore DM = \sqrt{10^2 - x^2}$$

1

$$\text{Area (A)} = \frac{1}{2} (10 + 10 + 2x) \sqrt{100 - x^2} = \frac{1}{2} (10 + x) \sqrt{100 - x^2}$$

1

$$\text{Let } S = A^2 = (10 + x)^2 (100 - x^2)$$

$$\frac{ds}{dx} = 0 \Rightarrow (10 + x)^2 (-2x) + (100 - x^2) 2(10 + x) = 0$$

1/2

$$(10 + x)^2 (-2x + 20 - 2x) = 0 \Rightarrow x = 5$$

1

$$\frac{d^2s}{dx^2} = (10 + x)^2 (-4) + (20 - 4x) 2(10 + x) < 0 \text{ at } x = 5$$

1

$$\therefore \text{ for Maximum area, } x = 5$$

1/2

$$\text{Maximum area} = 15\sqrt{75} = 75\sqrt{3} \text{ cm}^2$$

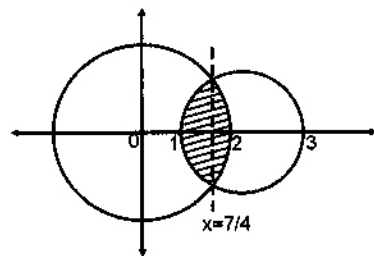
1

25. Correct figure

1

$$\text{Solving } x^2 + y^2 = 4 \text{ and } (x - 2)^2 + y^2 = 1$$

$$\text{we get } x = \frac{7}{4}$$



1

$$\therefore \text{ Required area} = 2 \left[ \int_{7/4}^2 \int \sqrt{4 - x^2} \, dx + \int_1^{7/4} \int \sqrt{1 - (x - 2)^2} \, dx \right]$$

1

$$= 2 \left[ \left[ \frac{x}{2} \sqrt{4 - x^2} + 2 \sin^{-1} \frac{x}{2} \right]_2^{7/4} + \left[ \frac{x - 2}{2} \sqrt{1 - (x - 2)^2} + \frac{1}{2} \sin^{-1} (x - 2) \right]_1^{7/4} \right]$$

1

$$= 2 \left[ \pi - \frac{7}{8} \frac{\sqrt{15}}{4} - 2 \sin^{-1} \frac{7}{8} + \left( -\frac{1}{8} \frac{\sqrt{15}}{4} + \frac{1}{2} \sin^{-1} \left( -\frac{1}{4} \right) + \frac{1}{2} \frac{\pi}{2} \right) \right]$$

1

$$= \frac{5\pi}{2} - \frac{\sqrt{15}}{2} - \sin^{-1} \left( \frac{1}{4} \right) - 4 \sin^{-1} \left( \frac{7}{8} \right) \text{ sq.u}$$

1

26. Here  $f(x) = (x^2+x+2)$ ,  $h = \frac{b-a}{n} = \frac{1}{n}$  ½

$$\int_1^2 f(x)dx = \lim_{n \rightarrow \infty} \frac{1}{n} [f(1) + f(1+h) + f(1+2h) + \dots + f[1+(n-1)h]]$$
 1

$$= \lim_{n \rightarrow \infty} \frac{1}{n} [4 + (4+3h+h^2) + (4+6h+4h^2) + \dots + (4+(n-1)3h+(n-1)^2h^2)]$$
 2

$$= \lim_{n \rightarrow \infty} \frac{1}{n} \left[ 4n + \frac{3}{n} \cdot \frac{n(n-1)}{2} + \frac{1}{n^2} \frac{n(n-1)(2n-1)}{6} \right]$$
 1½

$$= \lim_{n \rightarrow \infty} \left[ 4 + \frac{3}{2} \left( 1 - \frac{1}{n} \right) + \frac{1}{6} \left( 1 - \frac{1}{n} \right) \left( 2 - \frac{1}{n} \right) \right]$$
 ½

$$= 4 + \frac{3}{2} + \frac{1}{3} = \frac{24+9+2}{6} = \frac{35}{6}$$
 ½

OR

put  $x = \sin \alpha$  and  $\sqrt{x} = \sin \beta$  ½

$$\therefore \sin^{-1}[x\sqrt{1-x} - \sqrt{x}\sqrt{1-x^2}] = \sin^{-1} [\sin \alpha \cos \beta - \cos \alpha \sin \beta]$$

$$= \sin^{-1}[\sin(\alpha-\beta)] = \alpha-\beta = \sin^{-1}x - \sin^{-1}\sqrt{x}$$
 ½

$$\therefore \text{Given integral} = \int_0^1 (\sin^{-1}x - \sin^{-1}\sqrt{x}) dx = \int_0^1 \sin^{-1}x dx - \int_0^1 \sin^{-1}\sqrt{x} dx$$
 1

$$= [x \cdot \sin^{-1}x]_0^1 - \frac{1}{2} \int_0^1 \frac{2x}{\sqrt{1-x^2}} dx - [x \cdot \sin^{-1}\sqrt{x}]_0^1 + \int_0^1 \frac{1}{\sqrt{1-x}} \cdot \frac{1}{2\sqrt{x}} \cdot x dx$$
 1

$$= \frac{\pi}{2} + [\sqrt{1-x^2}]_0^1 - \frac{\pi}{2} + \frac{1}{2} \int_0^1 \frac{\sqrt{x}}{\sqrt{1-x}} dx$$
 1

$$= -1 + \frac{1}{2} \int_1^0 \frac{-\sqrt{1-t^2} \cdot 2t dt}{t} \quad [1-x = t^2, dx = -2t dt]$$
 1

$$= -1 + \int_0^1 \sqrt{1-t^2} dt = 1 + \left[ \frac{t}{2} \sqrt{1-t^2} + \frac{1}{2} \sin^{-1}t \right]_0^1 = \left( -1 + \frac{\pi}{4} \right)$$
 1



27. Let Q be the foot of perpendicular from P to the plane and P'(x, y, z) be the image of P in the plane.

∴ The equations of line through P and Q is

$$\frac{x-1}{2} = \frac{y-3}{-1} = \frac{z-4}{1}$$

The coordinates of Q (for some value of  $\lambda$ ) are

$$(2\lambda+1, -\lambda+3, \lambda+4)$$

Since Q lies on the plane, ∴  $2(2\lambda+1) - 1(\lambda+3) + (\lambda+4) + 3 = 0$

Solving to get  $\lambda = -1$

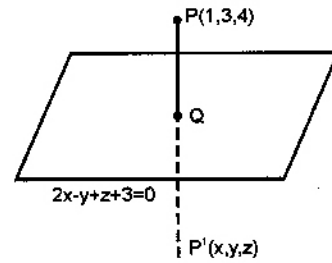
∴ coordinates of foot of perpendicular (Q) are (-1, 4, 3)

Perpendicular distance (PQ) =  $\sqrt{(2)^2 + (-1)^2 + (1)^2} = \sqrt{6}$  units

Since Q is mid point of PP'

$$\therefore \frac{x+1}{2} = -1, \frac{y+3}{2} = 4, \frac{z+4}{2} = 3 \Rightarrow x = -3, y = 5, z = 2$$

∴ Image of P is (-3, 5, 2)



1

1/2

1

1/2

1/2

1/2

28. Let, number of executive class tickets to be sold, be x and that of economy class be y.

∴ LPP becomes : Maximise Profit (P) =  $1000x + 600y$

Subject to :

$$\begin{aligned} x &\geq 0, y \geq 0 \\ x + y &\leq 200 \\ y &\geq 4x \text{ or } 4x - y \leq 0 \\ x &\geq 20 \end{aligned}$$

For correct graph

Getting vertices of feasible region as A(20, 180), B(40, 160), C(20, 80)

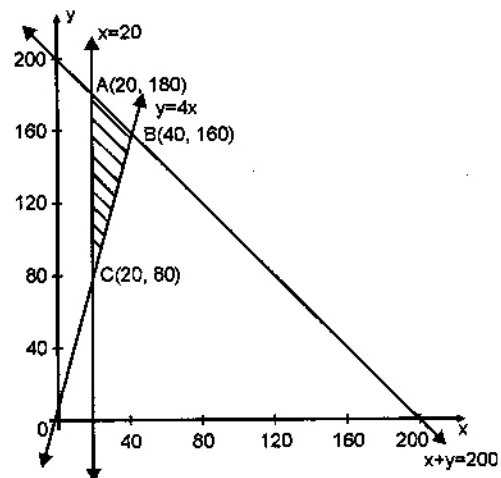
1/2

Profit at A = Rs. 128000

Profit at B = Rs. 136000

Profit at C = Rs. 68000

∴ Max profit = Rs. 136000 for 40 executive and 160 economy tickets



1 1/2

2

1

29. Let the events be defined as :

$E_1$  : Bag A is selected

$E_2$  : Bag B is selected

$E_3$  : Bag C is selected

A : A red ball is selected

$$\therefore P(E_1) = \frac{1}{6}, P(E_2) = \frac{2}{6} = \frac{1}{3} \text{ and } P(E_3) = \frac{3}{6} = \frac{1}{2}$$

$$P\left(\frac{A}{E_1}\right) = \frac{3}{5}, P\left(\frac{A}{E_2}\right) = \frac{3}{7} \text{ and } P\left(\frac{A}{E_3}\right) = \frac{4}{9}$$

$$P\left(\frac{E_2}{A}\right) = \frac{P(E_2)P\left(\frac{A}{E_2}\right)}{P(E_1)P\left(\frac{A}{E_1}\right) + P(E_2)P\left(\frac{A}{E_2}\right) + P(E_3)P\left(\frac{A}{E_3}\right)} = \frac{\frac{1}{3} \cdot \frac{3}{7}}{\frac{1}{6} \cdot \frac{3}{5} + \frac{1}{3} \cdot \frac{3}{7} + \frac{1}{2} \cdot \frac{4}{9}}$$
$$= \frac{90}{293}$$

**SAMPLE PAPER - II**

**MATHEMATICS**

**CLASS - XII**

**Time : 3 Hours**

**Max. Marks : 100**

**General Instructions**

1. All questions are compulsory.
2. The question paper consist of 29 questions divided into three sections A, B and C. Section A comprises of 10 questions of one mark each, section B comprises of 12 questions of four marks each and section C comprises of 07 questions of six marks each.
3. All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
4. There is no overall choice. However, internal choice has been provided in 04 questions of four marks each and 02 questions of six marks each. You have to attempt only one of the alternatives in all such questions.
5. Use of calculators in not permitted. You may ask for logarithmic tables, if required.

## SECTION A

1. Write the number of all one-one functions from the set  $A = \{a, b, c\}$  to itself.
2. Find  $x$  if  $\tan^{-1} 4 + \cot^{-1} x = \frac{\pi}{2}$
3. What is the value of  $|3I_3|$ , where  $I_3$  is the identity matrix of order 3?
4. For what value of  $k$ , the matrix  $\begin{bmatrix} 2-k & 3 \\ -5 & 1 \end{bmatrix}$  is not invertible?
5. If  $A$  is a matrix of order  $2 \times 3$  and  $B$  is a matrix of order  $3 \times 5$ , what is the order of matrix  $(AB)^T$  or  $T$ ?
6. Write a value of  $\int \frac{dx}{\sqrt{4-x^2}}$ .
7. Find  $f(x)$  satisfying the following :  
$$\int e^x (\sec^2 x + \tan x) dx = e^x f(x) + c$$
8. In a triangle  $ABC$ , the sides  $AB$  and  $BC$  are represented by vectors  $2\hat{i}-\hat{j}+2\hat{k}$ ,  $\hat{i}+3\hat{j}+5\hat{k}$  respectively. Find the vector representing  $CA$ .
9. Find the value of  $\lambda$  for which the vector  $\vec{a} = 3\hat{i}+\hat{j}-2\hat{k}$  and  $\vec{b} = \hat{i}+\lambda\hat{j}-3\hat{k}$  are perpendicular to each other.
10. Find the value of  $\lambda$  such that the line  $\frac{x-2}{9} = \frac{y-1}{\lambda} = \frac{z+3}{-6}$  is perpendicular to the plane  $3x-y-2z=7$

## SECTION B

11. Show that the function  $f: \mathbb{R} \rightarrow \mathbb{R}$  defined by  $f(x) = 2x^3 - 7$ , for  $x \in \mathbb{R}$  is bijective.

OR

Let  $f, g: \mathbb{R} \rightarrow \mathbb{R}$  be defined as  $f(x) = |x|$  and  $g(x) = [x]$  where  $[x]$  denotes the greatest integer less than or equal to  $x$ . Find  $f \circ g \left( \frac{5}{2} \right)$  and  $g \circ f \left( -\sqrt{2} \right)$ .

12. Prove that  $\tan^{-1} 1 + \tan^{-1} 2 + \tan^{-1} 3 = \pi$

13. If  $A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix}$ , show that  $A^2 - 5A - 14I = 0$ . Hence find  $A^{-1}$ .

14. Show that  $f(x) = |x-3|$ ,  $\forall x \in \mathbb{R}$ , is continuous but not differentiable at  $x=3$ .

OR

If  $\tan \left( \frac{x^2 - y^2}{x^2 + y^2} \right) = a$ , then prove that  $\frac{dy}{dx} = \frac{y}{x}$

15. Verify Rolle's Theorem for the function  $f$ , given by  $f(x) = e^x (\sin x - \cos x)$  on  $\left[ \frac{\pi}{4}, \frac{5\pi}{4} \right]$

16. Using differentials, find the approximate value of  $\sqrt{25.2}$

OR

Two equal sides of an isosceles triangle with fixed base 'a' are decreasing at the rate of 9 cm/second. How fast is the area of the triangle decreasing when the two sides are equal to 'a'.

17. Evaluate  $\int_{-1}^{\frac{1}{2}} |x \cos(\pi x)| dx$ .

18. Solve the following differential equation :

$$ye^{\frac{x}{y}} dx = (xe^{\frac{x}{y}} + y) dy$$

19. Solve the following differential equation :

$$(1+y+x^2y)dx + (x+x^3)dy = 0, \text{ where } y=0 \text{ when } x=1$$

20. If  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are three unit vectors such that  $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c} = 0$  and angle between  $\vec{b}$  and  $\vec{c}$  is  $\frac{\pi}{6}$ , prove that  $\vec{a} = \pm 2(\vec{b} \times \vec{c})$ .

21. Show that the four points  $(0, -1, -1)$ ,  $(4, 5, 1)$ ,  $(3, 9, 4)$  and  $(-4, 4, 4)$  are coplanar. Also, find the equation of the plane containing them.

22. A coin is biased so that the head is 3 times as likely to occur as tail. If the coin is tossed three times, find the probability distribution of number of tails.

OR

How many times must a man toss a fair coin, so that the probability of having at least one head is more than 80%?

## SECTION C

23. Using properties of determinants, show that

$$\Delta = \begin{vmatrix} (b+c)^2 & ab & ca \\ ab & (a+b)^2 & bc \\ ac & bc & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$

24. The sum of the perimeter of a circle and a square is  $k$ , where  $k$  is some constant. Prove that the sum of their areas is least when the side of square is double the radius of the circle.

OR

A helicopter is flying along the curve  $y = x^2 + 2$ . A soldier is placed at the point  $(3, 2)$ . Find the nearest distance between the soldier and the helicopter.

25. Evaluate :  $\int \frac{1}{\sin x (5-4 \cos x)} dx$

OR

Evaluate :  $\int \sqrt{\frac{1-\sqrt{x}}{1+\sqrt{x}}} dx$

26. Using integration, find the area of the region

$$\{(x, y) : |x-1| \leq y \leq \sqrt{5-x^2}\}$$

27. Show that the lines  $\frac{x+3}{-3} = \frac{y-1}{1} = \frac{z-5}{5}$  and  $\frac{x+1}{-1} = \frac{y-2}{2} = \frac{z-5}{5}$  are coplanar. Also find the equation of the plane.

28. From a pack of 52 cards, a card is lost. From the remaining 51 cards, two cards are drawn at random (without replacement) and are found to be both diamonds. What is the probability that the lost card was a card of heart?

29. A diet for a sick person must contain at least 4000 units of vitamins, 50 units of minerals and 1400 calories. Two foods X and Y are available at a cost of Rs 4 and Rs 3 per unit respectively. One unit of food X contains 200 units of vitamins, 1 unit of minerals and 40 calories, whereas 1 unit of food Y contains 100 units of vitamins, 2 units of minerals and 40 calories. Find what combination of foods X and Y should be used to have least cost, satisfying the requirements. Make it an LPP and solve it graphically.

**MARKING SCHEME**  
**MATHEMATICS CLASS - XII**  
**SAMPLE PAPER II**

**SECTION A**

1. 6
2. 4
3. 27
4. 17
5.  $5x^2$

6.  $\sin^{-1}\left(\frac{x}{2}\right)$

7.  $\tan x$

8.  $-(3\hat{i}+2\hat{j}+7\hat{k})$

9.  $\lambda = -9$

10.  $\lambda = -3$

(1 mark for correct answer for Qs. 1 to 10)

**SECTION B**

11. Let  $x, y$  be any two elements of  $R$  (domain)

$$\text{then } f(x) = f(y) \Rightarrow 2x^3 - 7 = 2y^3 - 7$$

$$\Rightarrow x^3 = y^3 \Rightarrow x = y \quad 1$$

so,  $f$  is an injective function

Let  $y$  be any element of  $R$  (co-domain)

$$\therefore f(x) = y \Rightarrow 2x^3 - 7 = y$$

$$\Rightarrow x^3 = \frac{y+7}{2} \Rightarrow x = \left(\frac{y+7}{2}\right)^{\frac{1}{3}}$$

Now for all  $y \in R$  (co-domain), there exists  $x = \left(\frac{y+7}{2}\right)^{\frac{1}{3}} \in R$  (domain) 1

$$\text{such that } f(x) = f\left\{\left(\frac{y+7}{2}\right)^{\frac{1}{3}}\right\} = 2\left\{\left(\frac{y+7}{2}\right)^{\frac{1}{3}}\right\}^3 - 7$$

$$= 2 \cdot \frac{y+7}{2} - 7 = y \quad 1$$

so,  $f$  is surjective

Hence,  $f$  is a bijective function

OR

$$f \circ g \left( \frac{5}{2} \right) = f \left[ g \left( \frac{5}{2} \right) \right] = f(2) = |2| = 2 \quad 2$$

$$g \circ f (-\sqrt{2}) = g [f (-\sqrt{2})] = g [ -\sqrt{2} ] = g [\sqrt{2}] = 1 \quad 2$$

12. L.H.S. =  $\tan^{-1}1 + \tan^{-2}2 + \tan^{-1}3$

$$= \frac{\pi}{4} + \frac{\pi}{2} - \cot^{-1}2 + \frac{\pi}{2} - \cot^{-1}3 \quad \frac{1}{2}$$

$$= \frac{5\pi}{4} - \tan^{-1} \left( \frac{1}{2} \right) - \tan^{-1} \left( \frac{1}{3} \right) \frac{1}{2}$$

$$= \frac{5\pi}{4} - \left( \tan^{-1} \frac{1}{2} + \tan^{-1} \frac{1}{3} \right) \quad \frac{1}{2}$$

$$= \frac{5\pi}{4} - \tan^{-1} \left( \frac{\frac{1}{2} + \frac{1}{3}}{1 - \frac{1}{2} \cdot \frac{1}{3}} \right) \quad 1$$

$$= \frac{5\pi}{4} - \tan^{-1} (1) \quad \frac{1}{2}$$

$$= \frac{5\pi}{4} - \frac{\pi}{4} \quad \frac{1}{2}$$

$$= \pi = \text{RHS} \quad \frac{1}{2}$$

13.  $A = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix} \Rightarrow A^2 = \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix} \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix} = \begin{bmatrix} 29 & -25 \\ -20 & 24 \end{bmatrix} \quad 1$

$$A^2 - 5A - 14I = \begin{bmatrix} 29 & -25 \\ -20 & 24 \end{bmatrix} - 5 \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix} - 14 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad \frac{1}{2}$$

$$= \begin{bmatrix} 29 & -25 \\ -20 & 24 \end{bmatrix} + \begin{bmatrix} -15 & 25 \\ 20 & -10 \end{bmatrix} + \begin{bmatrix} -14 & 0 \\ 0 & -14 \end{bmatrix}$$



$$\begin{bmatrix} 29-15-14 & -25+25-0 \\ -20+20+0 & 24-10-14 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} = 0$$

1

Premultiplying  $A^2 - 5A - 14I = 0$  by  $A^{-1}$ , we get

$$A^{-1} \cdot A^2 - 5A^{-1}A - 14A^{-1}I = 0$$

$$\text{or, } A - 5I - 14A^{-1} = 0$$

½

$$\text{or } A^{-1} = \frac{1}{14} (A - 5I) = \frac{1}{14} \left\{ \begin{bmatrix} 3 & -5 \\ -4 & 2 \end{bmatrix} + \begin{bmatrix} -5 & 0 \\ 0 & -5 \end{bmatrix} \right\}$$

$$= \frac{1}{14} \begin{bmatrix} -2 & -5 \\ -4 & -3 \end{bmatrix}$$

1

$$14. \quad f(x) = |(x-3)| \Rightarrow f(x) = \begin{cases} x-3 & \text{if } x \geq 3 \\ -(x-3) & \text{if } x < 3 \end{cases}$$

½

$$\lim_{x \rightarrow 3^-} f(x) = \lim_{x \rightarrow 3^-} -(x-3) = 0$$

½

$$\lim_{x \rightarrow 3^+} f(x) = \lim_{x \rightarrow 3^+} (x-3) = 0$$

½

$$\text{and } f(3) = 3-3 = 0$$

$$\lim_{x \rightarrow 3^-} f(x) = \lim_{x \rightarrow 3^+} f(x) = f(3)$$

∴  $f(x)$  is continuous at  $x = 3$

½

For differentiability

$$Lf'(3) = \lim_{x \rightarrow 3^-} \frac{f(x) - f(3)}{x-3} = \lim_{x \rightarrow 3^-} \frac{-(x-3) - 0}{x-3} = -1$$

½

$$Rf'(3) = \lim_{x \rightarrow 3^+} \frac{f(x) - f(3)}{x-3} = \lim_{x \rightarrow 3^+} \frac{(x-3) - 0}{x-3} = 1$$

½

$$\therefore Lf'(3) \neq Rf'(3)$$

so,  $f(x)$  is not differentiable at  $x=3$

1

OR

$$\tan \left( \frac{x^2 - y^2}{x^2 + y^2} \right) = a$$